

# Substitution and per-residue selection in B cell affinity maturation

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<http://matsen.fhcrc.org/>

# Jenner's 1796 vaccine



Where are we 200 years later?

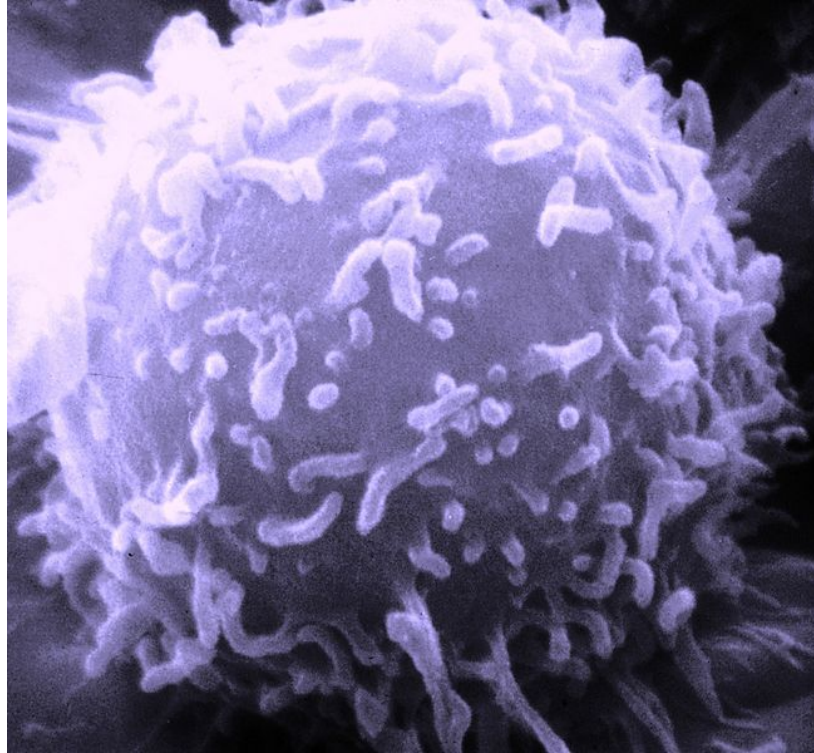
# RV144 HIV trial: 2003-2009

- 26,676 volunteers enrolled
- 16,395 volunteers randomized
- 125 infections
- \$105,000,000 and 6 years (!!)

Prospective studies are expensive, slow, and entail complex moral issues. This does not lend itself to rapid vaccine development.

*How might we guide vaccine development without disease exposure?*

# Vaccines manipulate the adaptive immune system

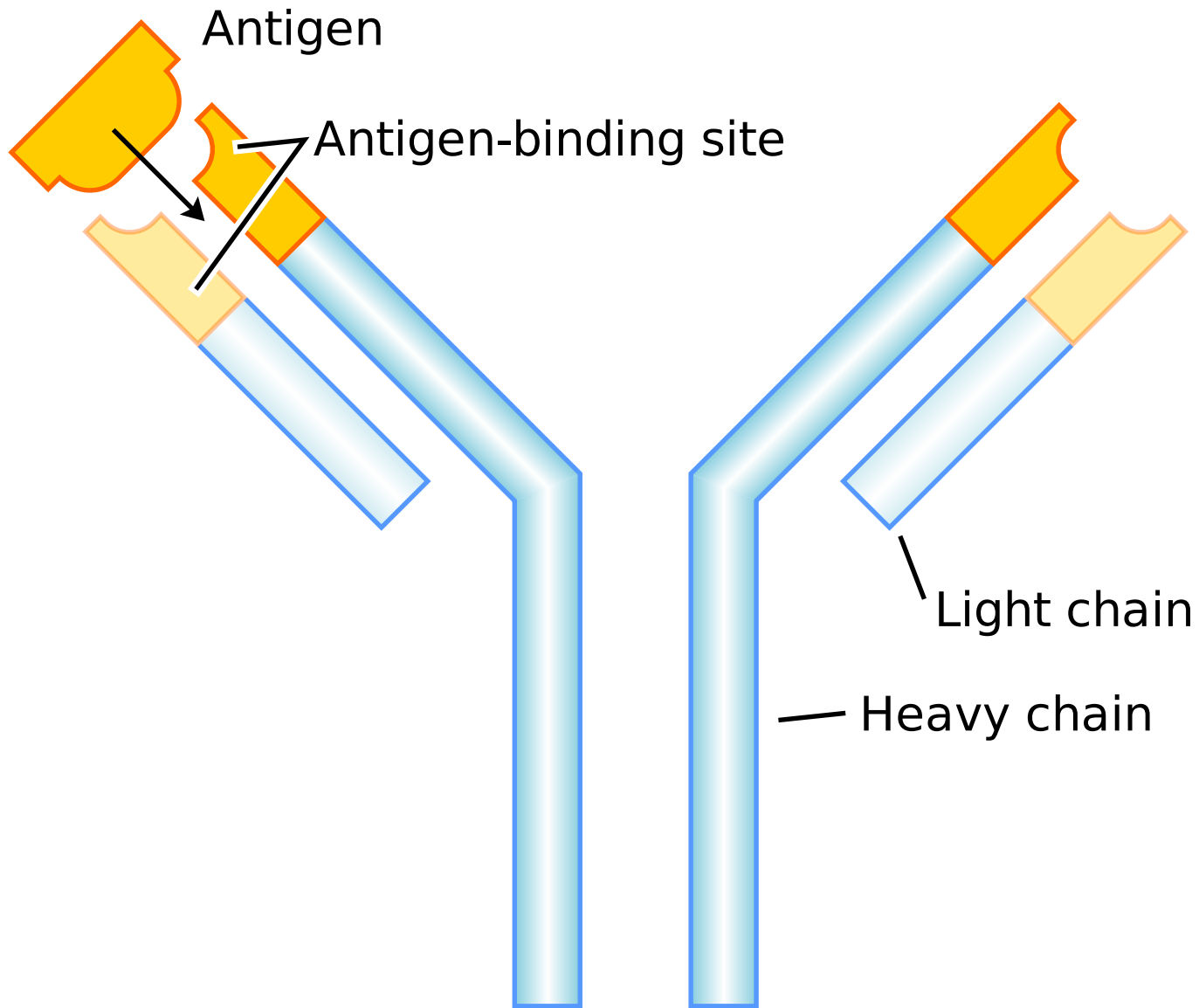


Antibody-making B cells: a key part of adaptive immunity.

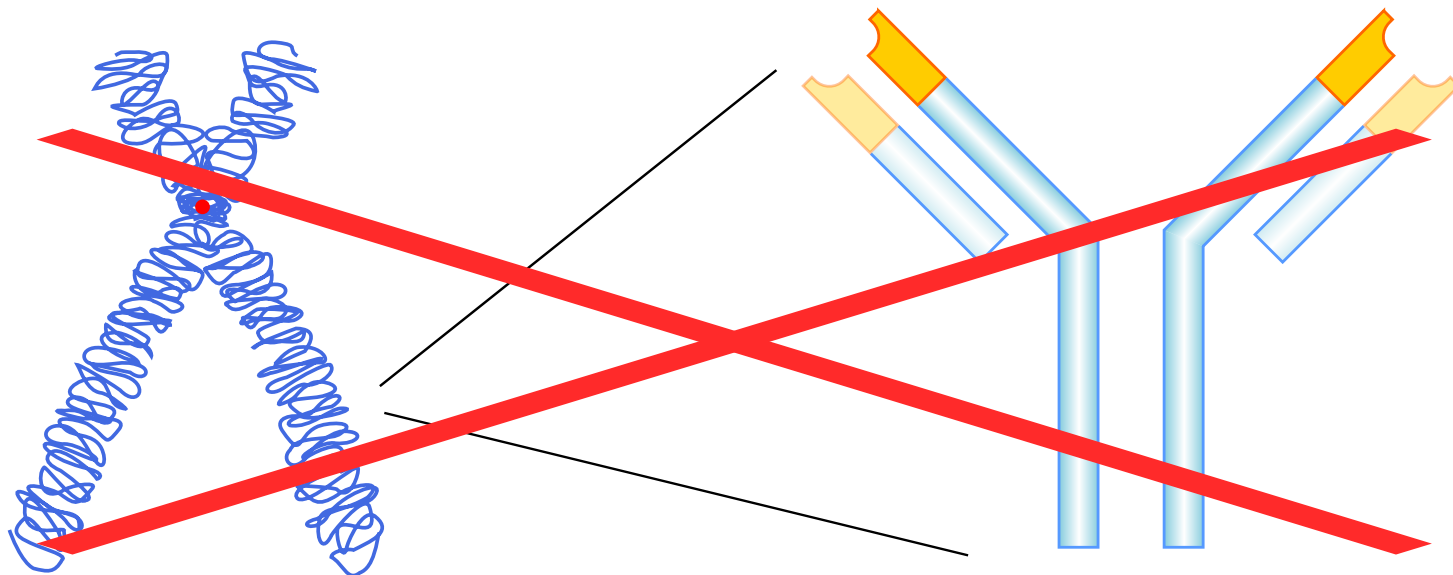
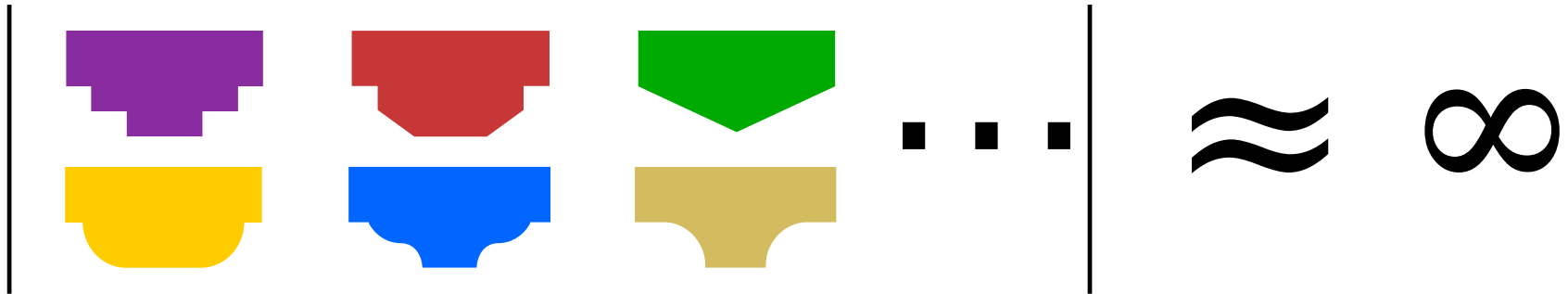
What can we learn from B cells without battle-testing them?

# Biological background

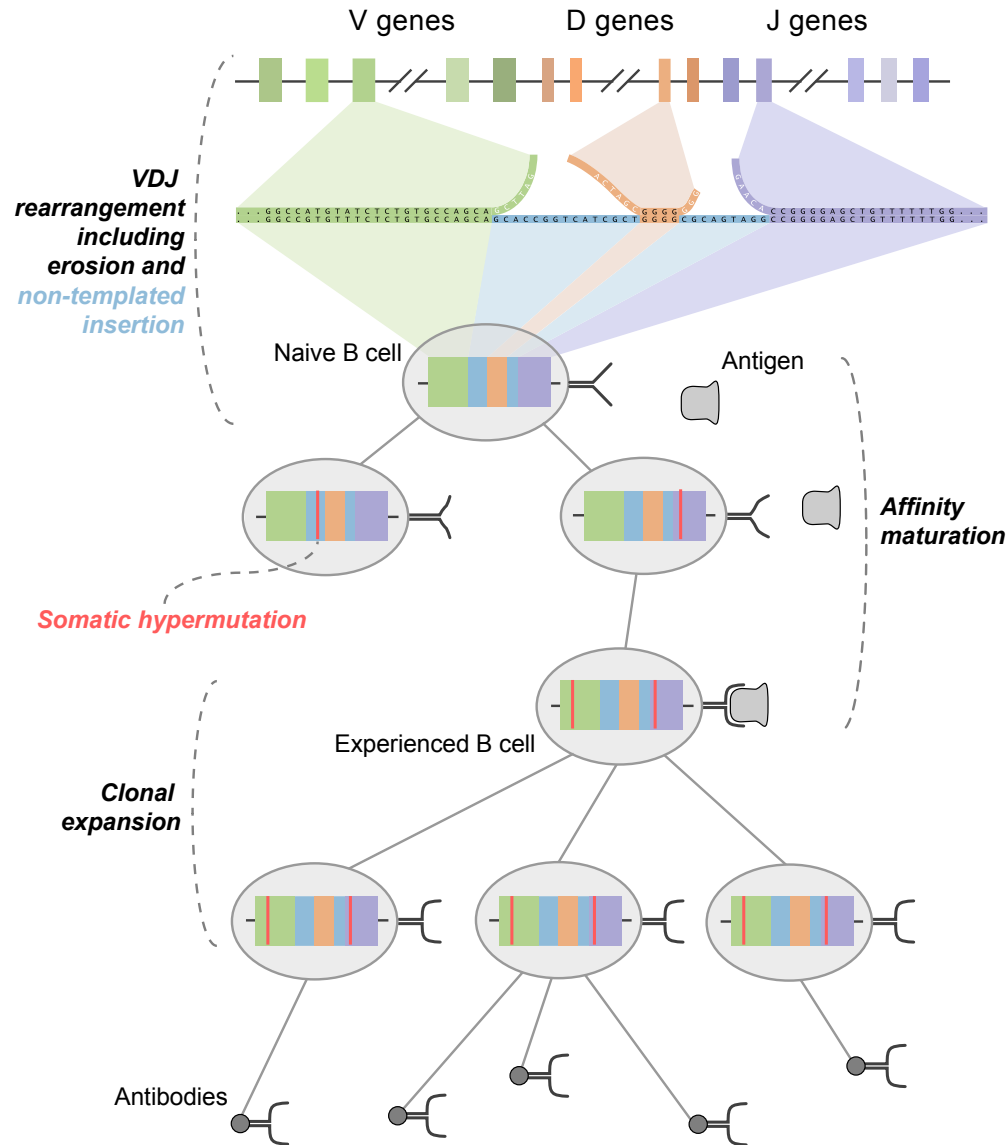
# Antibodies bind antigens



Too many antigens to code for directly

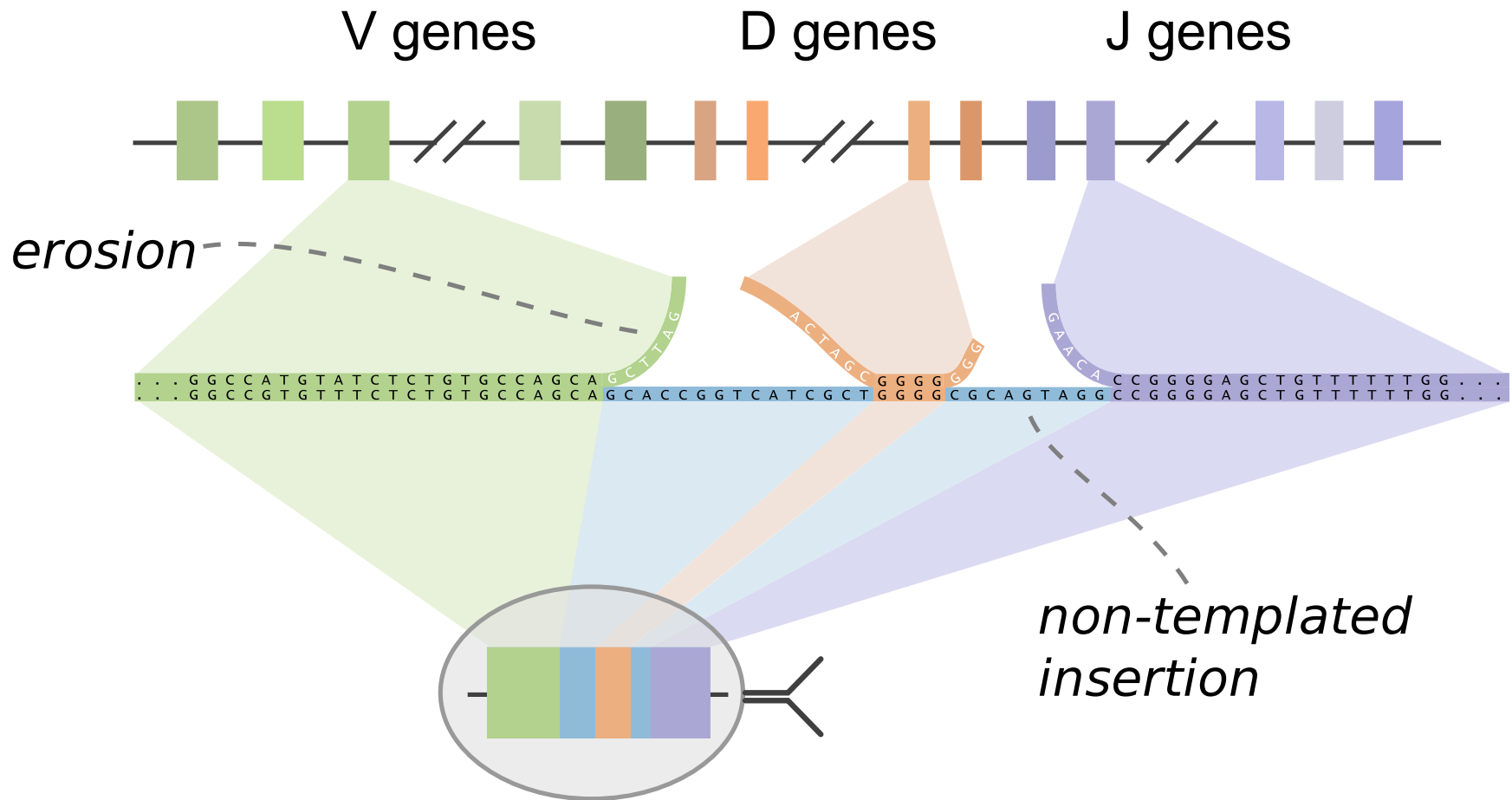


# B cell diversification process

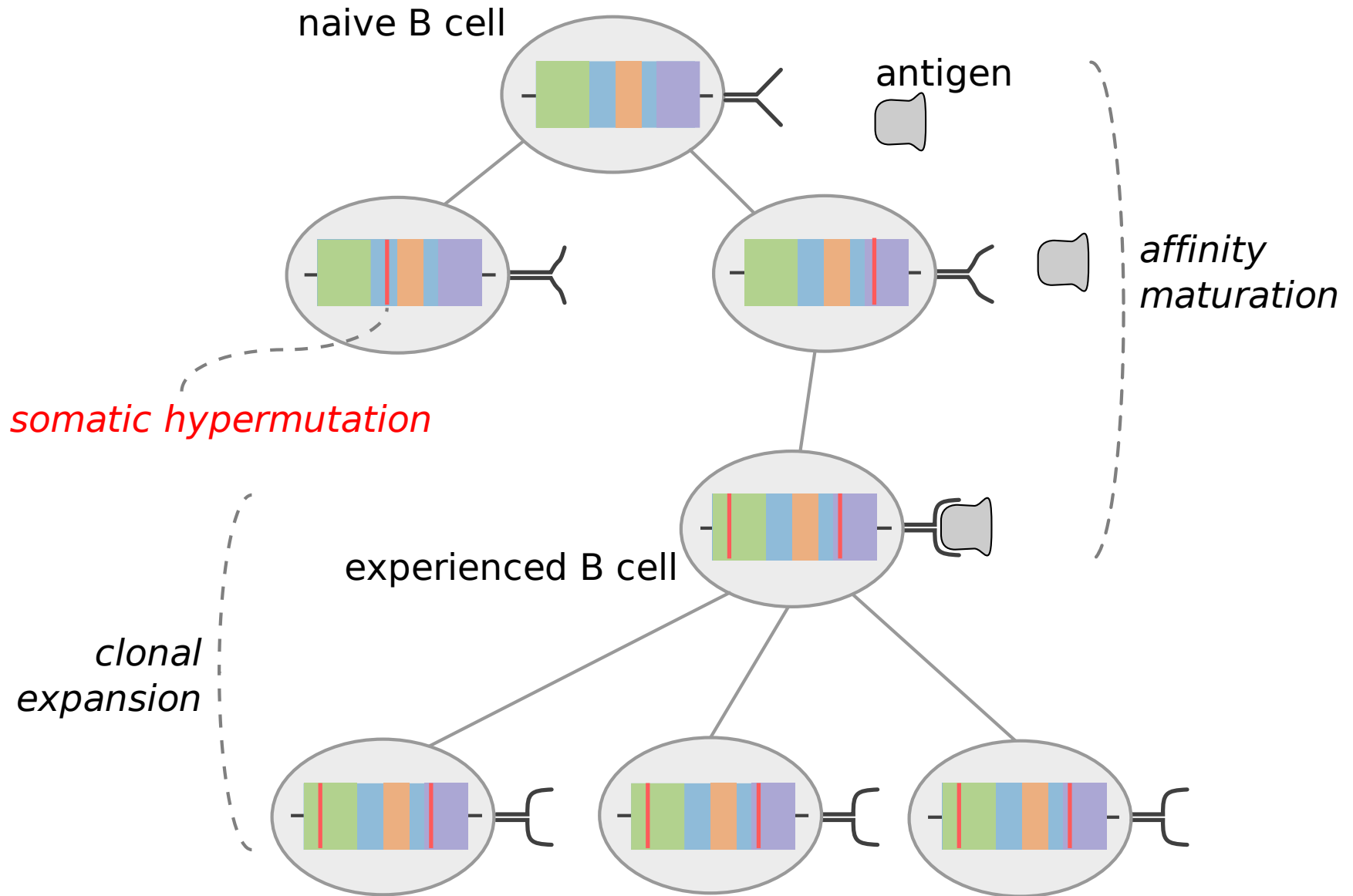




# B cell diversification overview

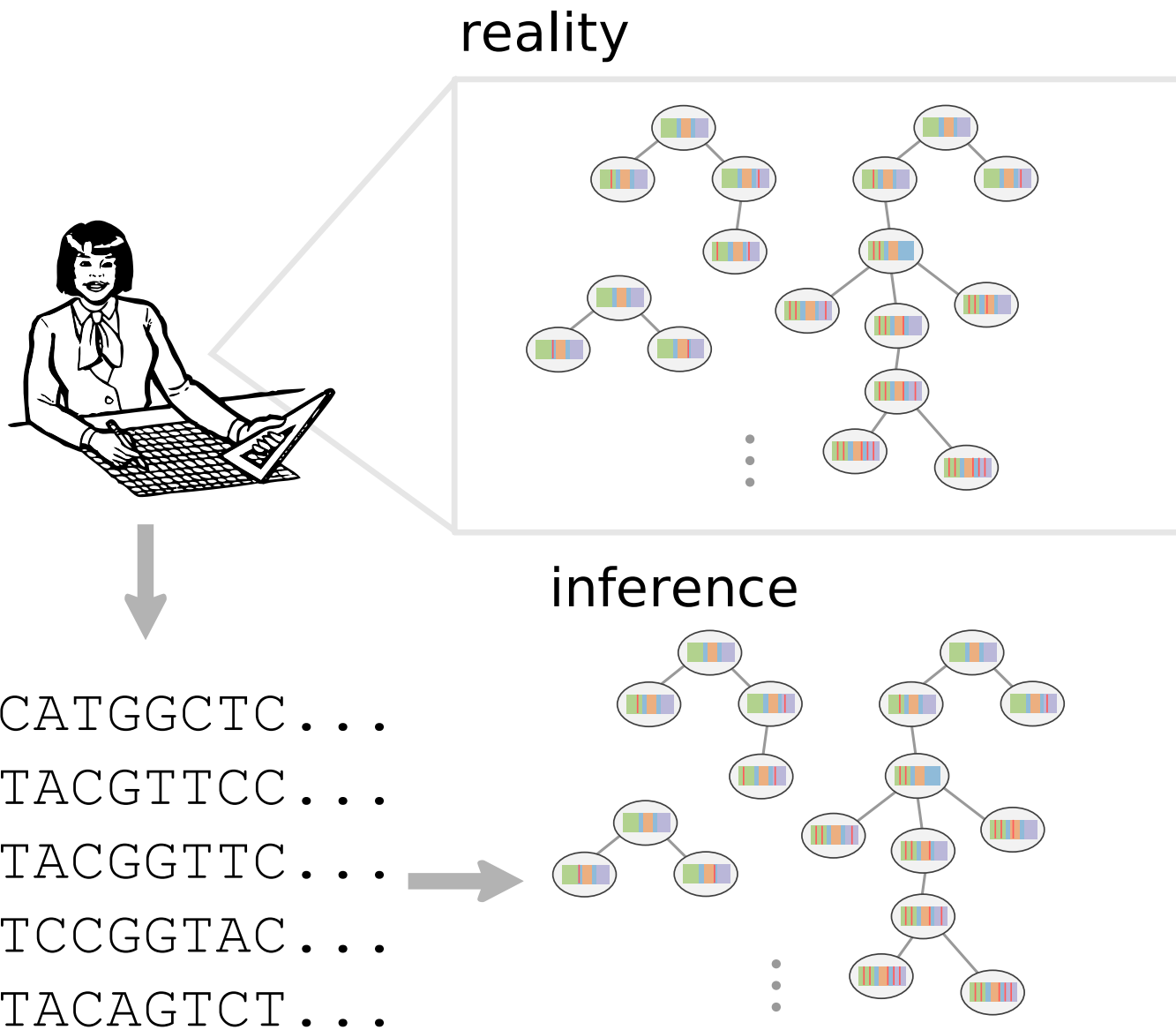


# B cell diversification overview

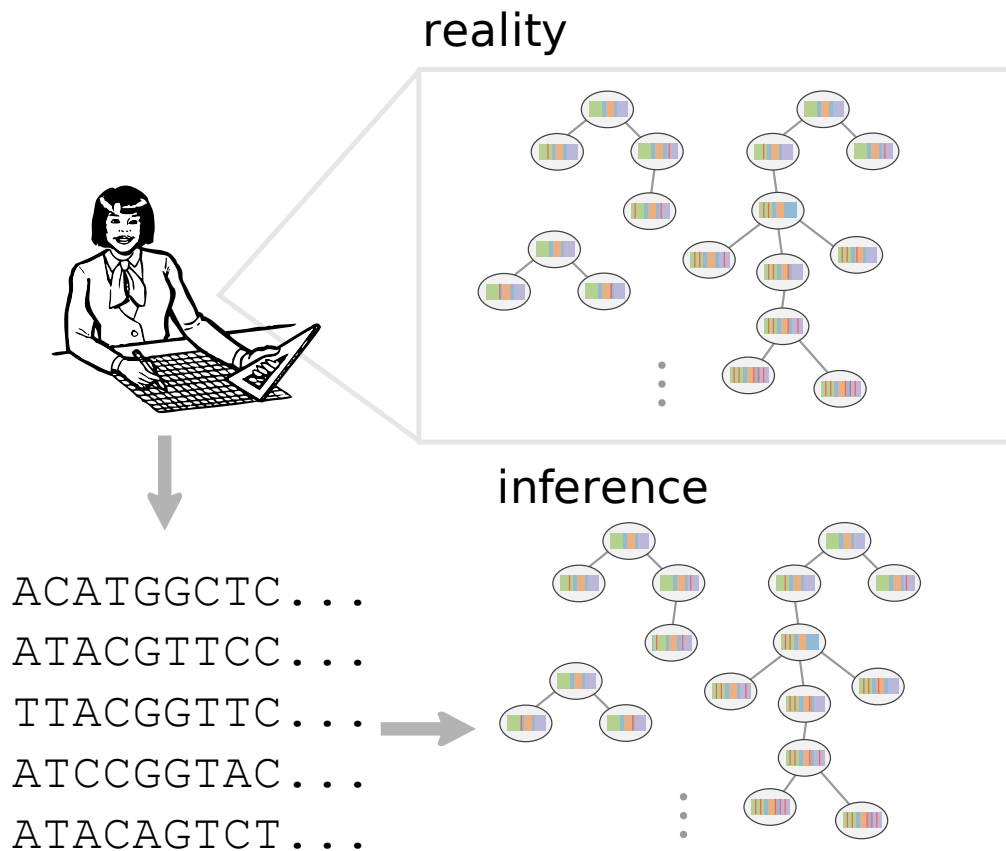


# Outline

# Goal 1: infer immune *history*



# Part 1 of talk: find appropriate substitution models

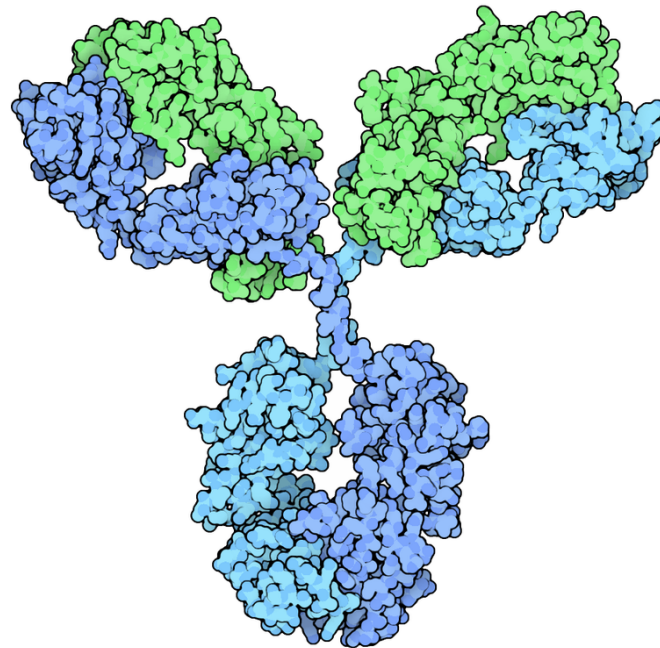


These are needed for likelihood-based phylogenetic inference.

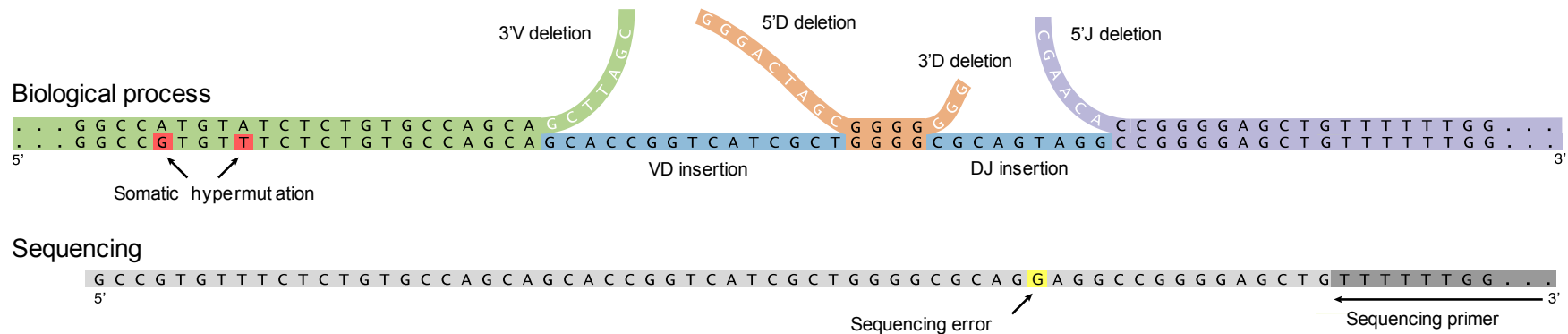
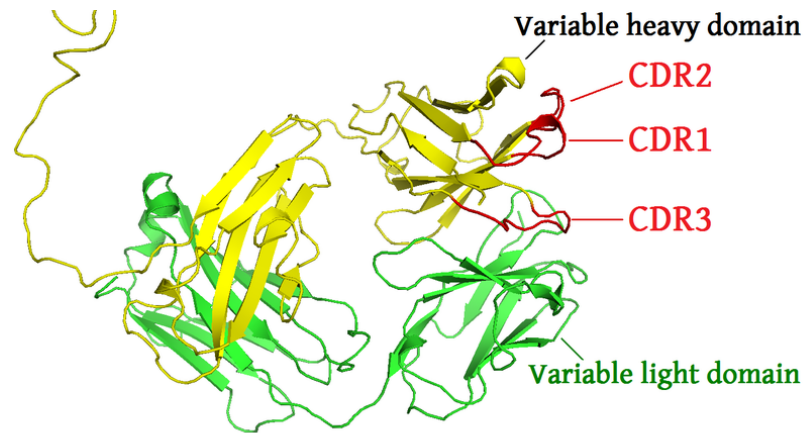
Goal 2: understand how we might *manipulate* immune repertoire with interventions

Which sites can be changed?

Part 2 of talk: natural selection inference



# The data: sequences from the CDR3 locus



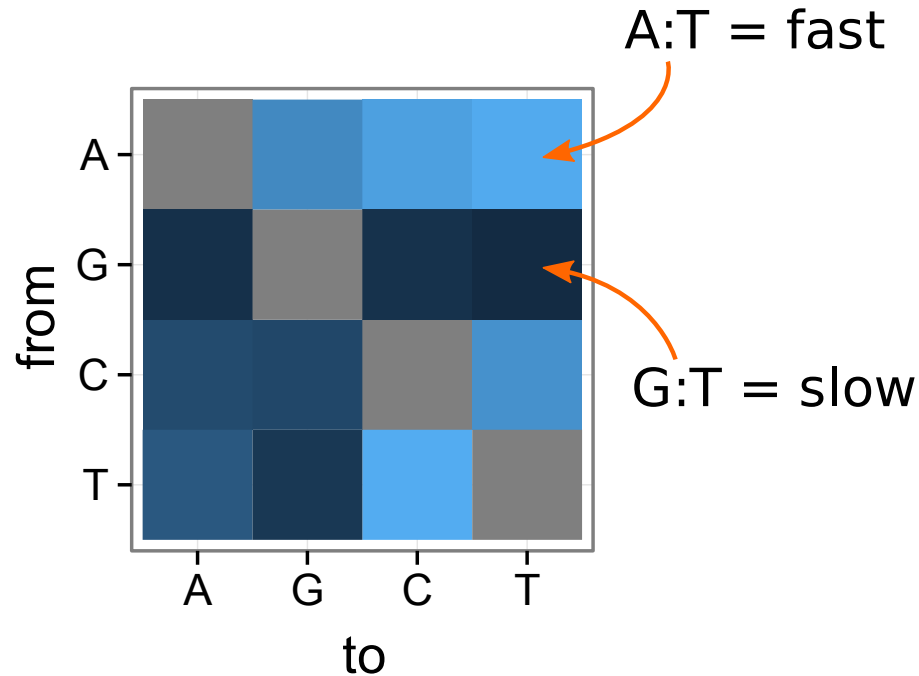
**Plenty:** a total of about 15 million unique 130nt sequences from memory B cell populations of three healthy individuals A, B, and C.

# Part 1



# Goal 1: Understand determinants of molecular evolution

Investigate overall mutation patterns of the B cell repertoire.



Models like this are used throughout phylogenetic inference.

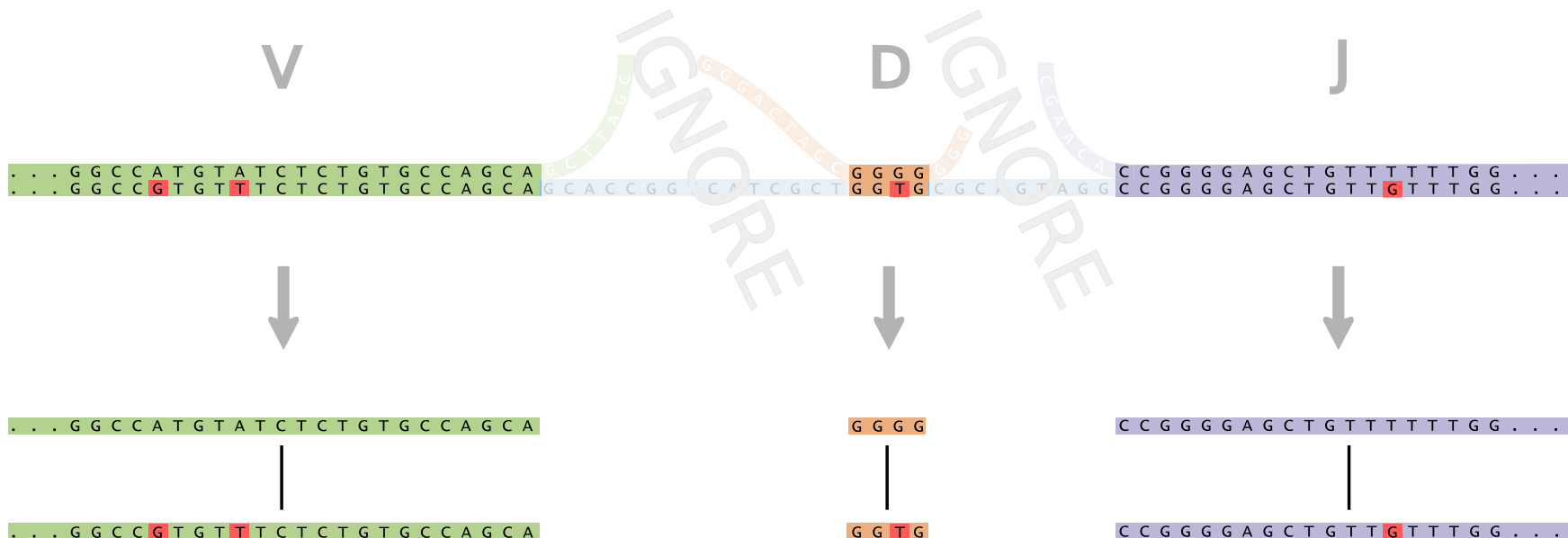
Not all BCRs share ancestry

In fact, most don't.

This is different from traditional phylogenetics.

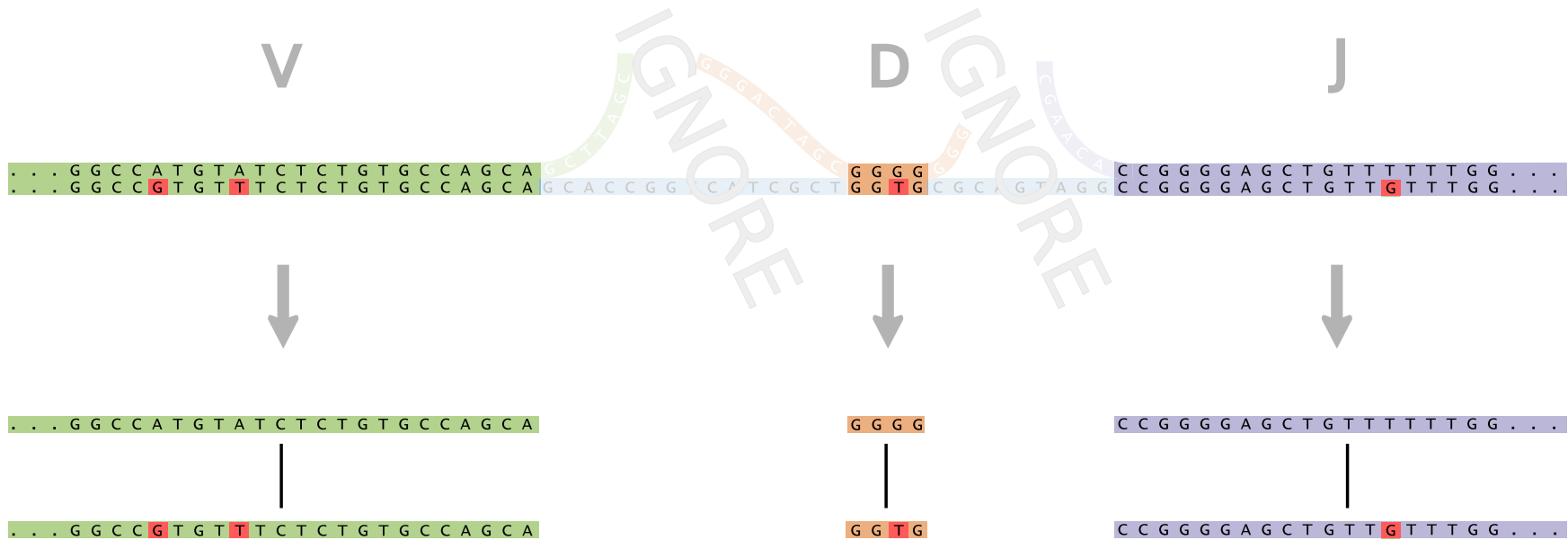
# Use two taxon “trees” for model fitting

*But:* we know ancestral state within V, D, J.



Our “trees” have an observed read on the bottom and the corresponding “ancestral” germline sequence on top, connected by a branch, representing some amount of divergence.

# Collection of two taxon "trees" for model fitting



We will test various models for the V, D, and J segments to select an appropriate evolutionary model for somatic hypermutation to eventually use in phylogenetic inference.

First question: do segments evolve differently?

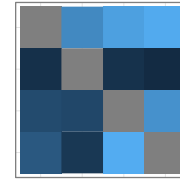
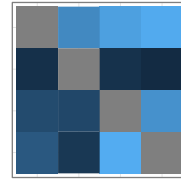
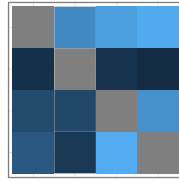
# Simple model

V

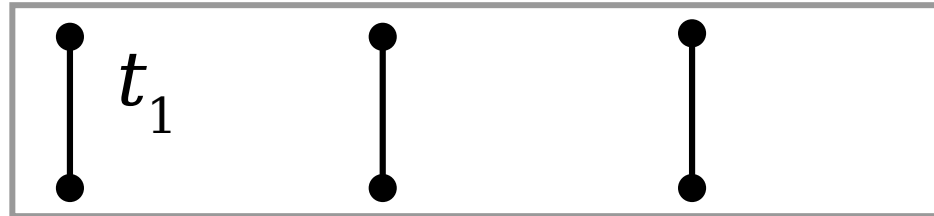
D

J

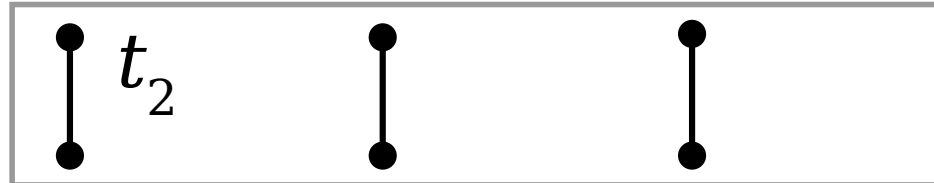
Mutation  
Model



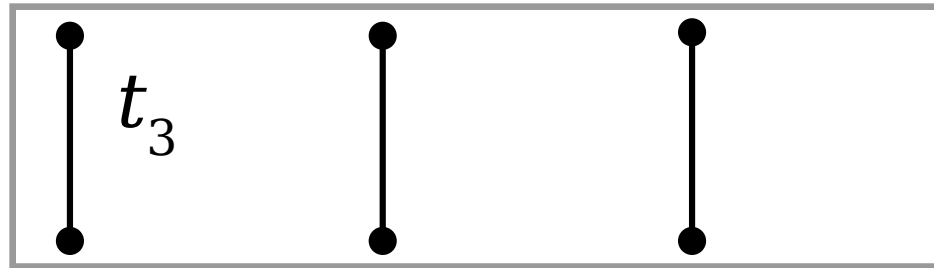
Seq. 1



Seq. 2



Seq. 3



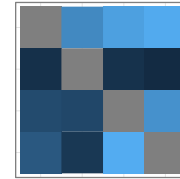
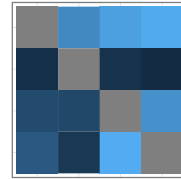
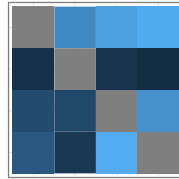
... more complex (i)

V

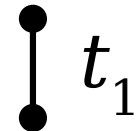
D

J

Mutation  
Model



Seq. 1



$t_1$

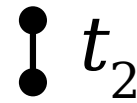


$r_D t_1$



$r_J t_1$

Seq. 2



$t_2$

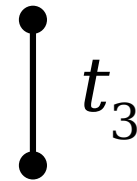


$r_D t_2$



$r_J t_2$

Seq. 3



$t_3$

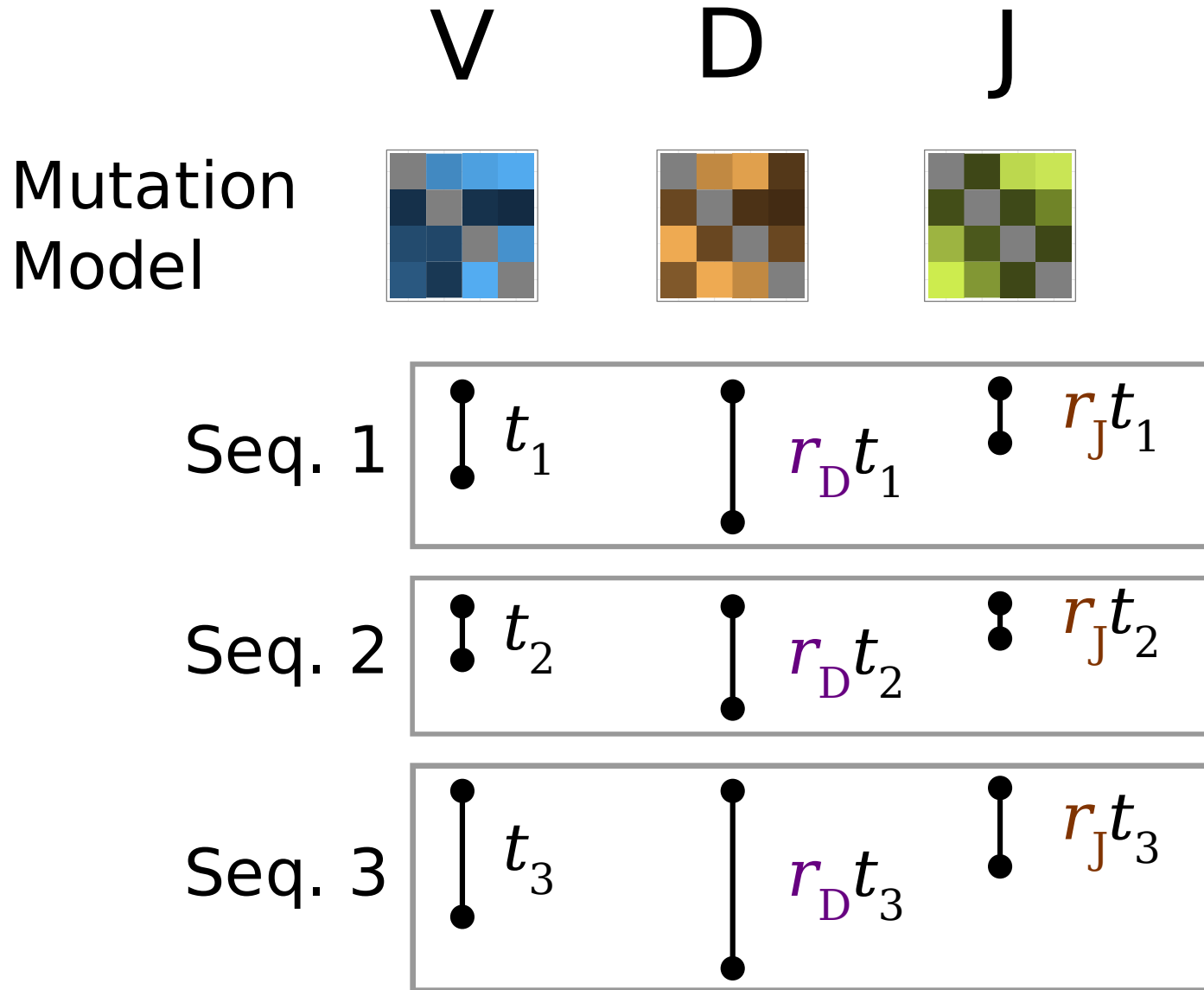


$r_D t_3$

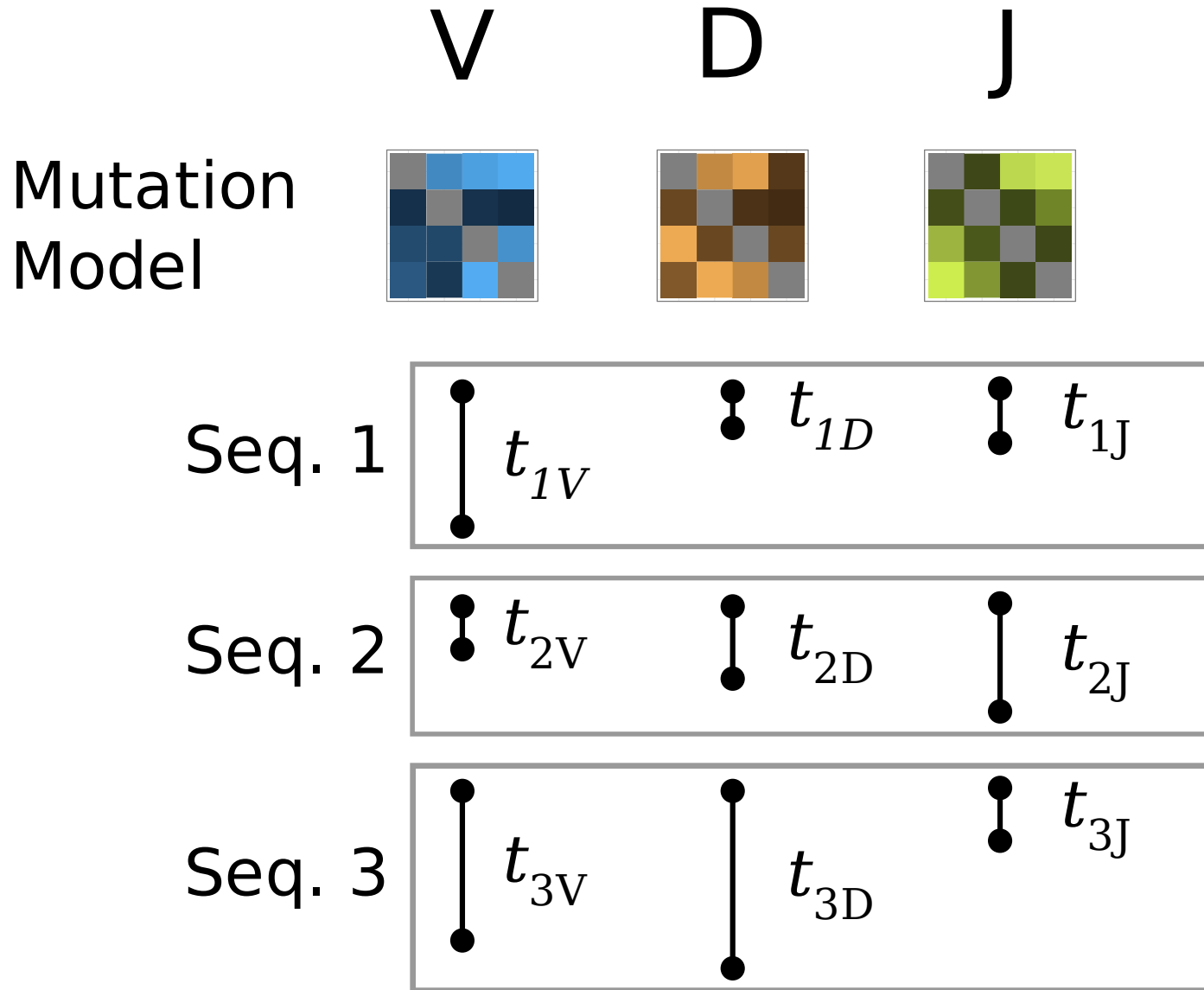


$r_J t_3$

... more complex (ii)

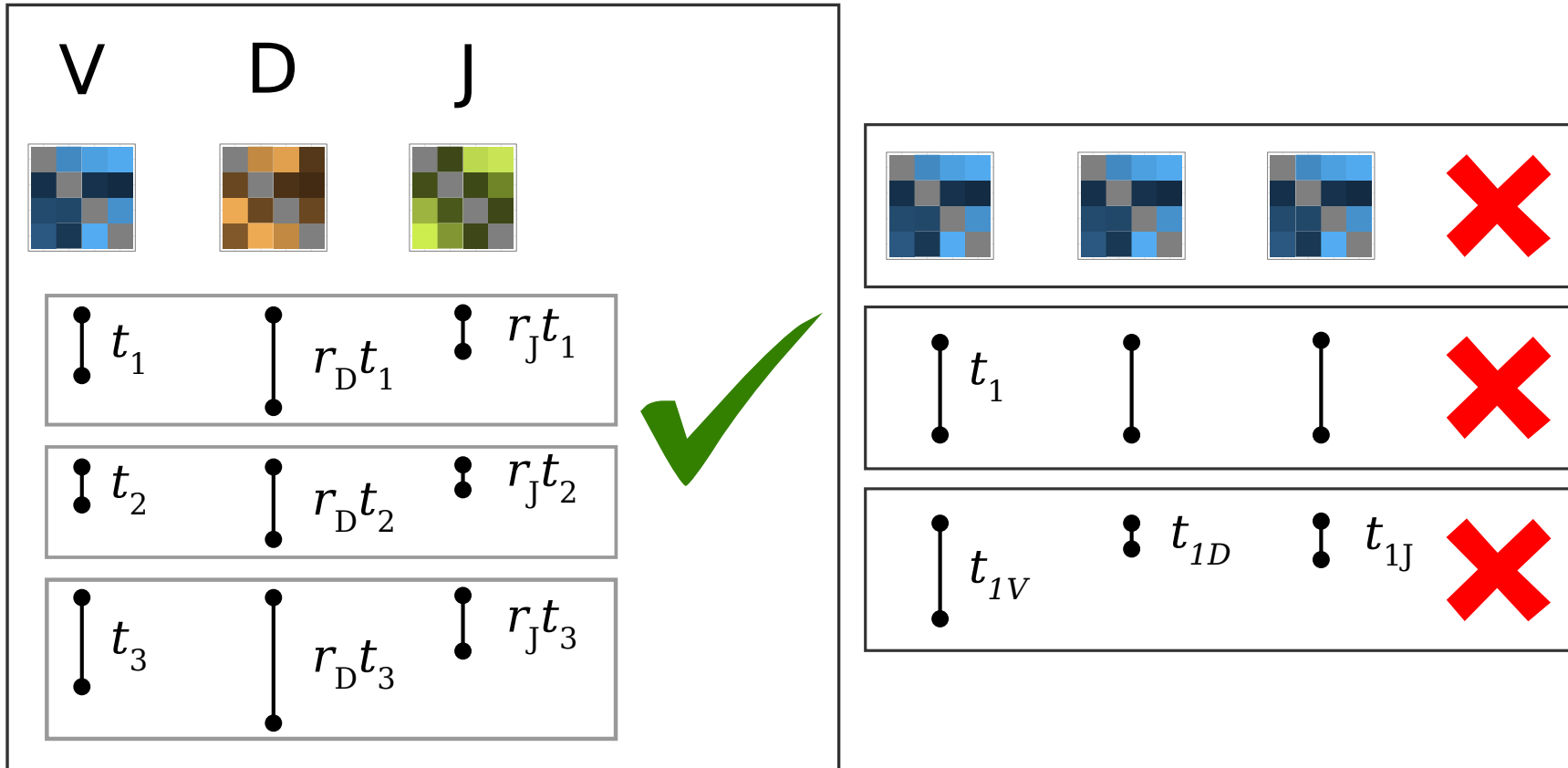


... most complex



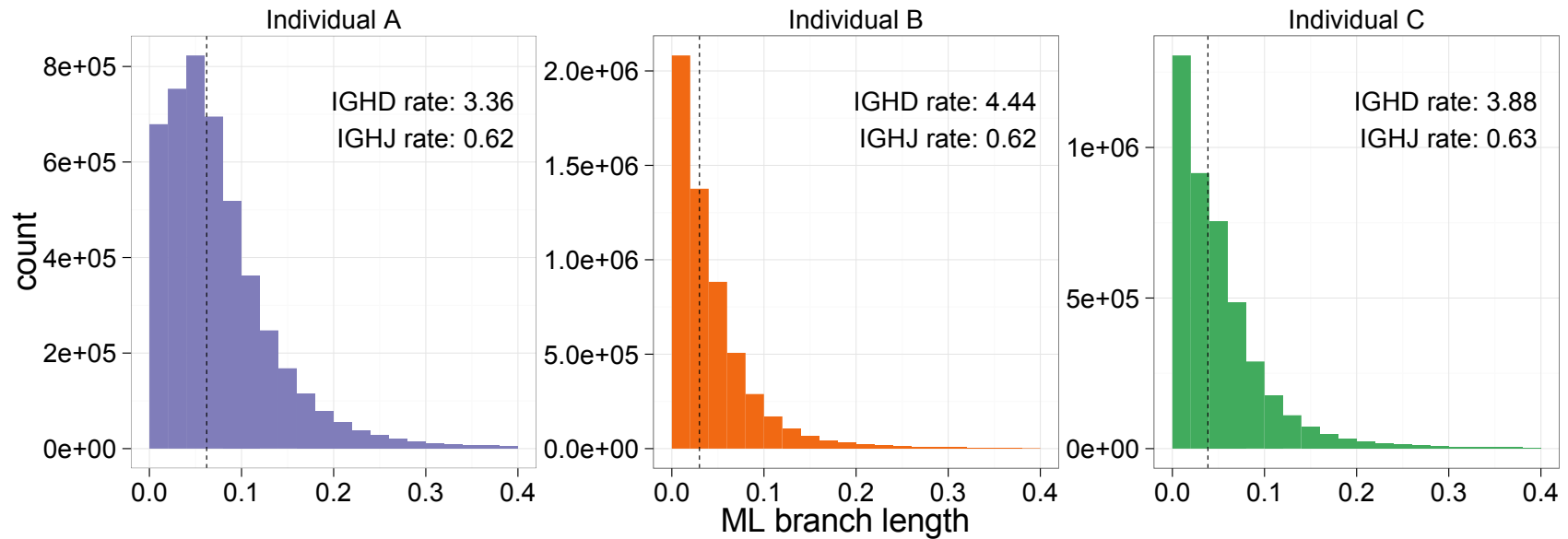


# Model testing results



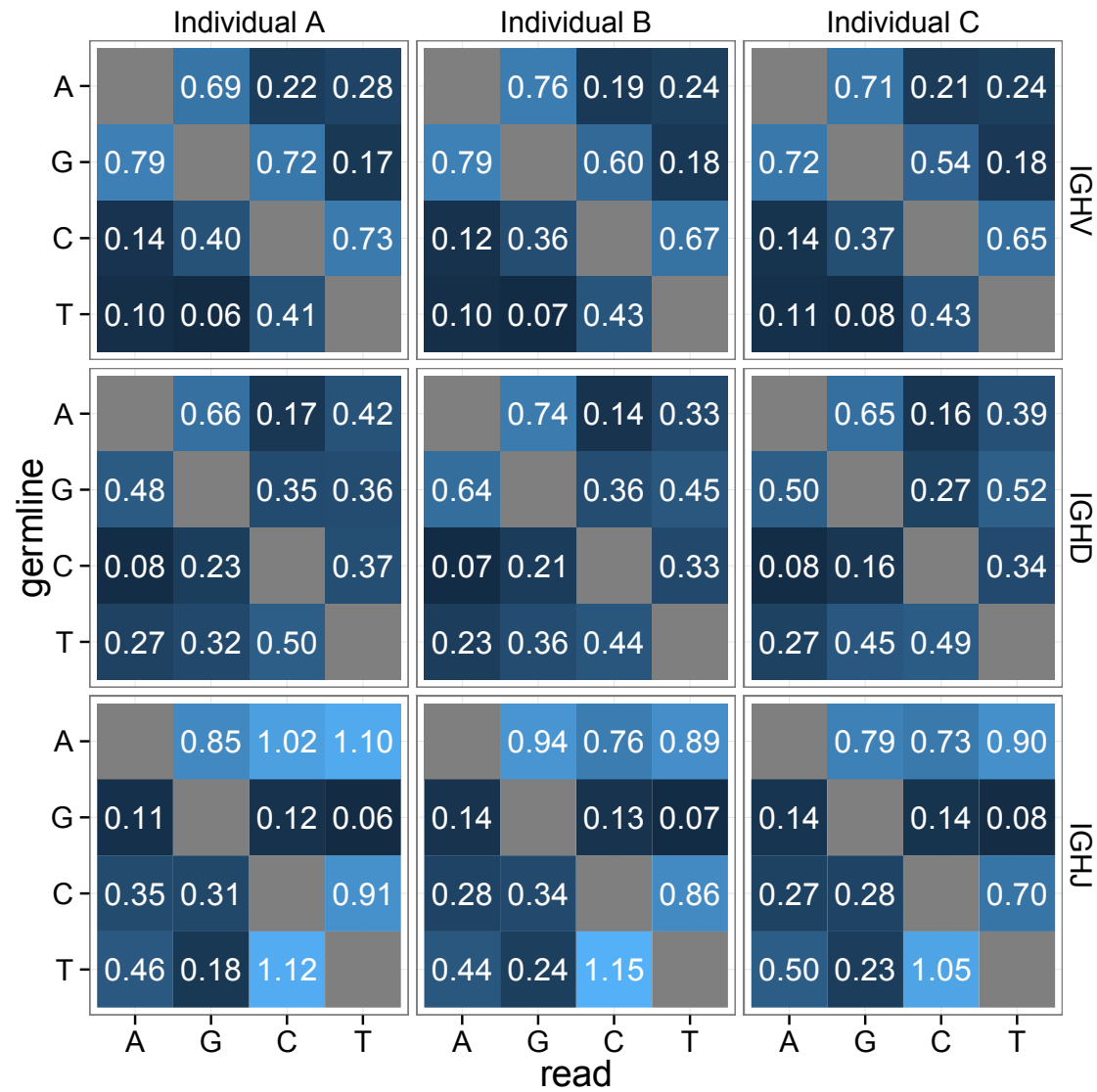
Identical model ranking across individuals (using AIC / BIC).

# Branch length distribution under this best model

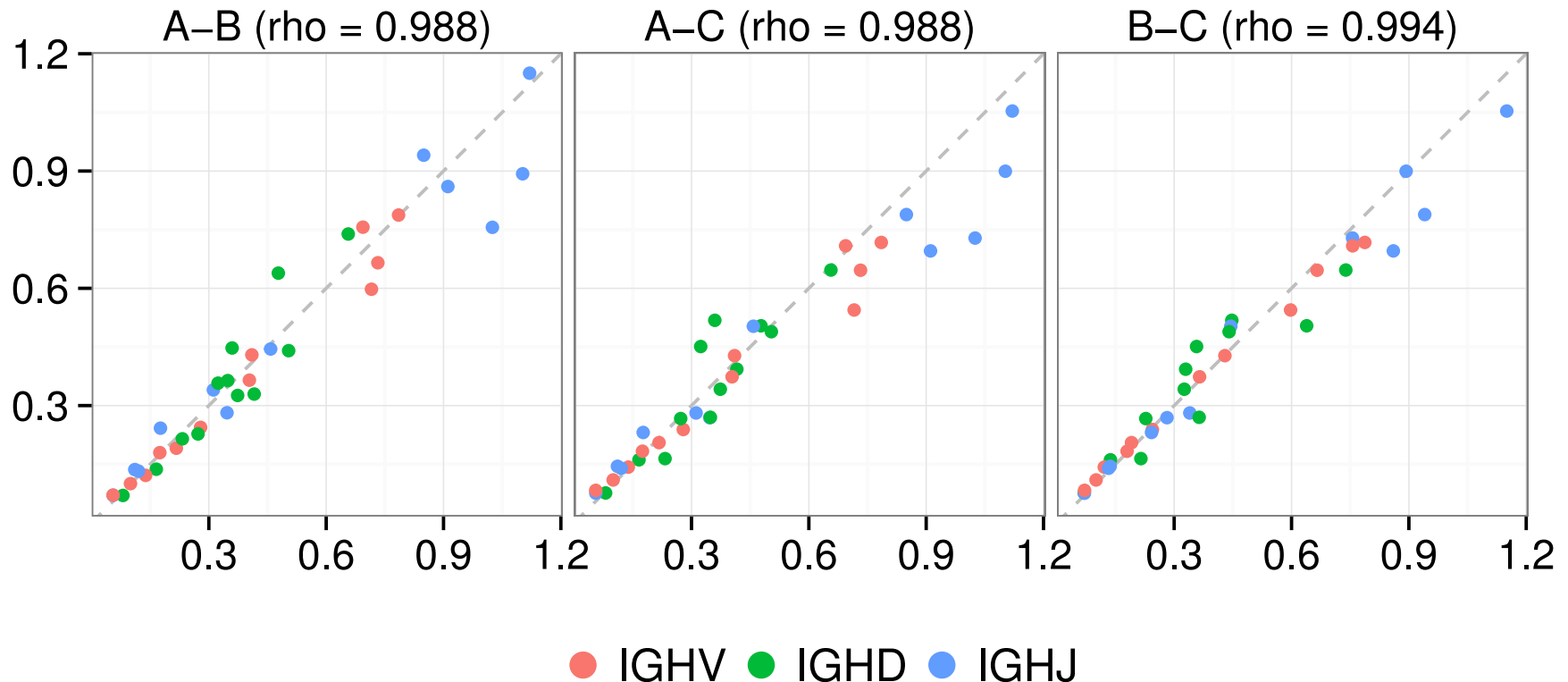


- **D** segments evolve substantially *faster* than **V**
- **J** segments evolve more *slowly* than **V**
- Individual A has a higher mutational load.

# Rate matrices for General Time Reversible model



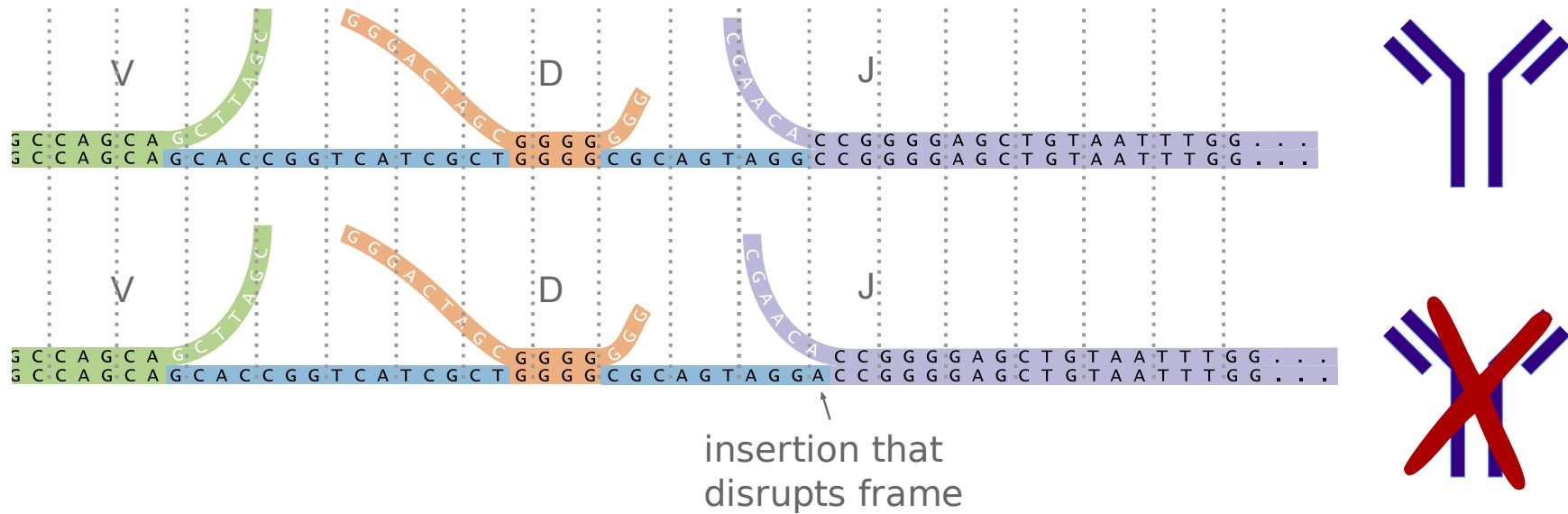
# Estimates of the mutational process are quite consistent between individuals



(each point is a single entry for one of the matrices for a pair of individuals.)

# (Important) aside: productive versus out-of-frame receptors

Each cell may carry two IGH alleles, but only one is expressed.



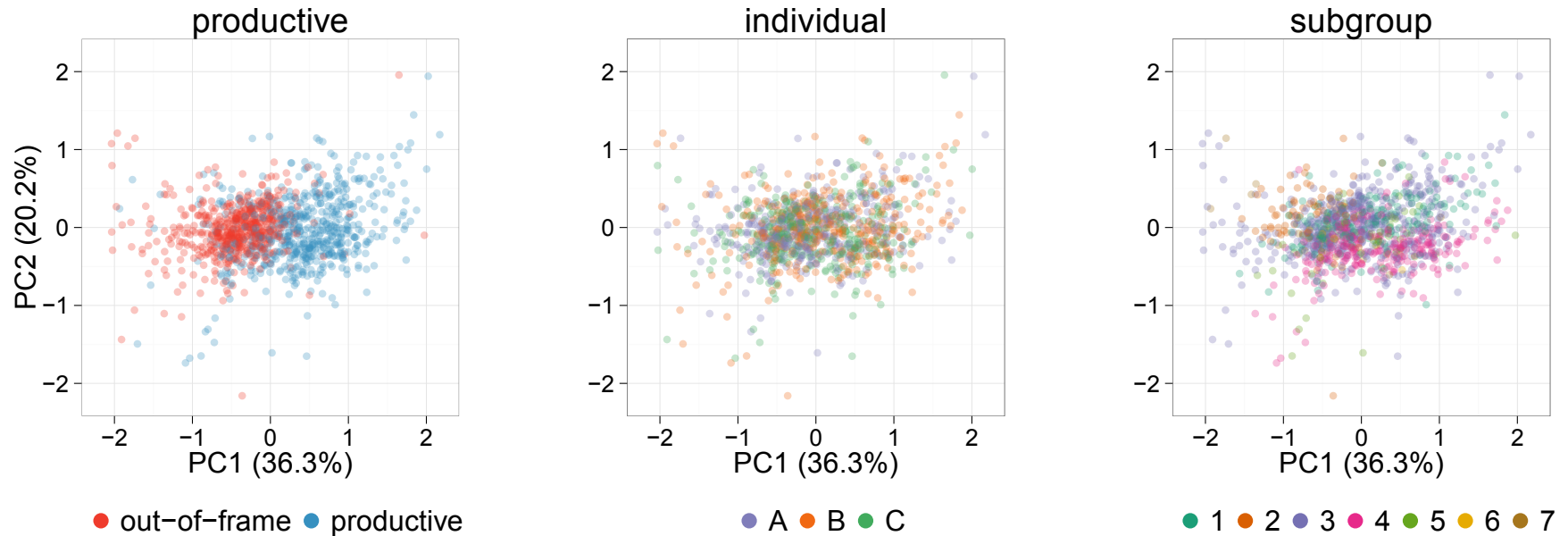
Next: what determines mutational processes of different IGHV genes?

Subdivide V genes:

- by individual (A, B, and C)
- by gene (V1-18, V2-3, etc)
- by productive / unproductive status

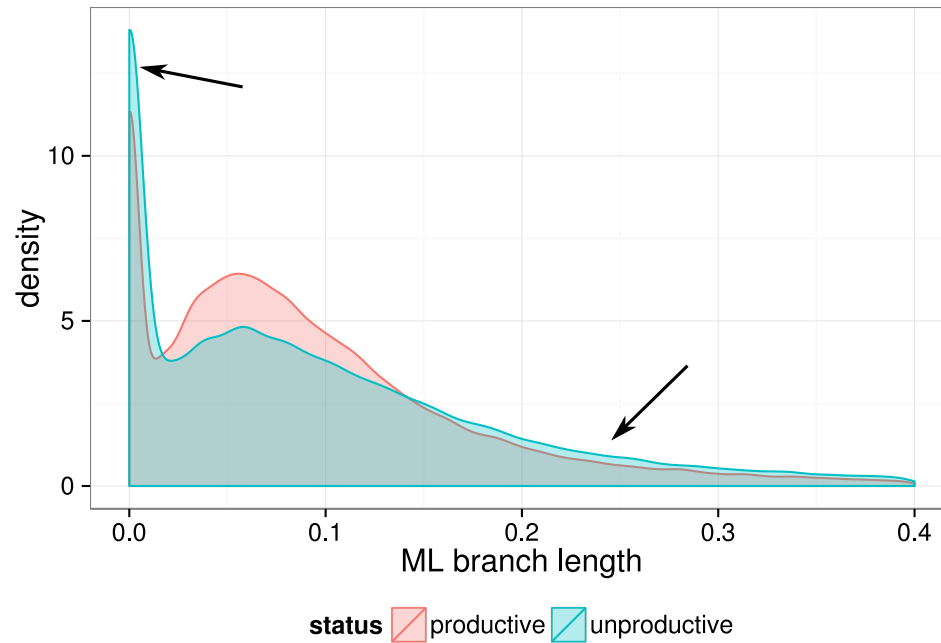
and fit each subset separately.

# Principal components analysis of individual IGHV GTR matrices



Inspired by the work of [\(Kosakovsky Pond \*et al\*, 2010\)](#) on evolutionary “fingerprinting.”

# Branch length differences between productive, unproductive



Unproductive rearrangements are more likely to be either:  
unchanged from germline, or more divergent.



# Wrap-up of Part 1

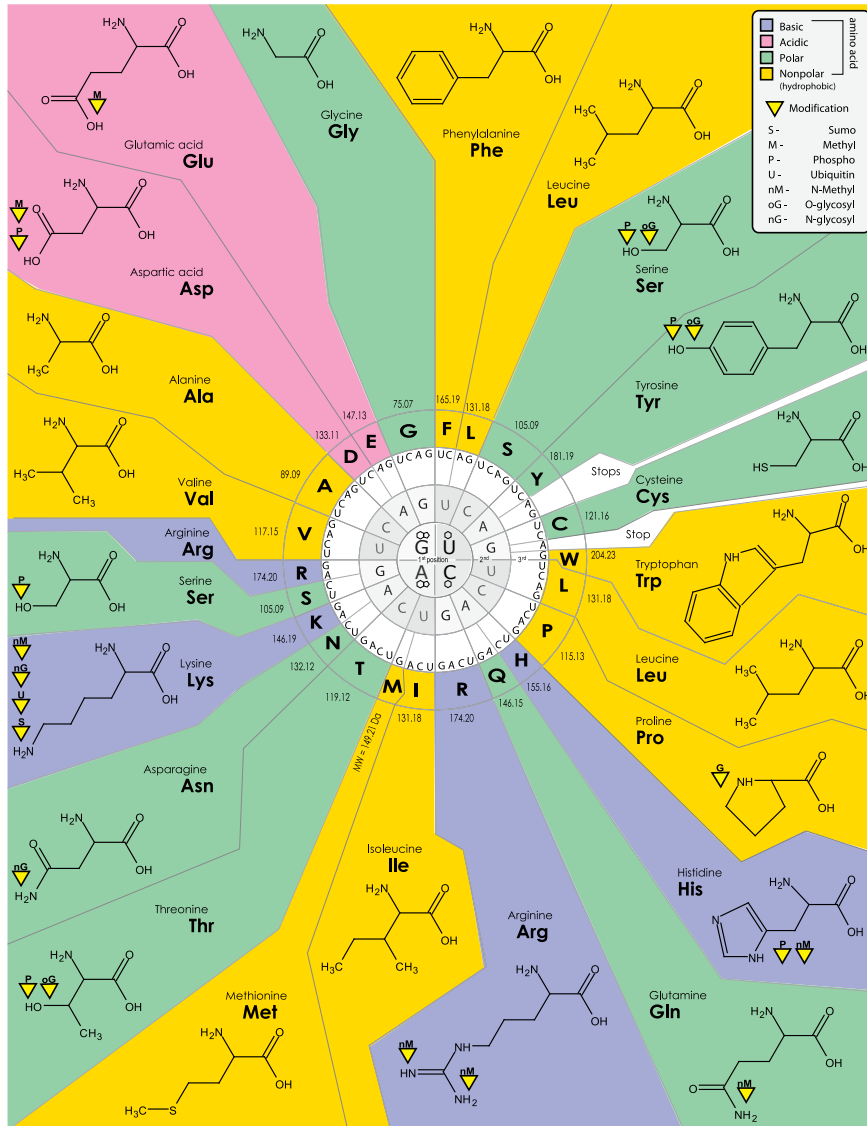
- We find that the data support a **moderately complex evolutionary model**; similar between individuals
- Mutation process of rearranged IGHV genes **primarily varies by in-frame/out-of-frame status**, with almost no per-individual signal and a bit of gene group-level signal

# Part 2

Goal 2: what if we want to mutate specific residues in an antibody. Is that allowed?

We can't answer that directly, but we can look across the repertoire at which *sites have tolerated change*.

# Genetic code degeneracy is a gift to molecular evolutionists enabling selection inference



Pro Pro

CCA → CCT  
*synonymous*

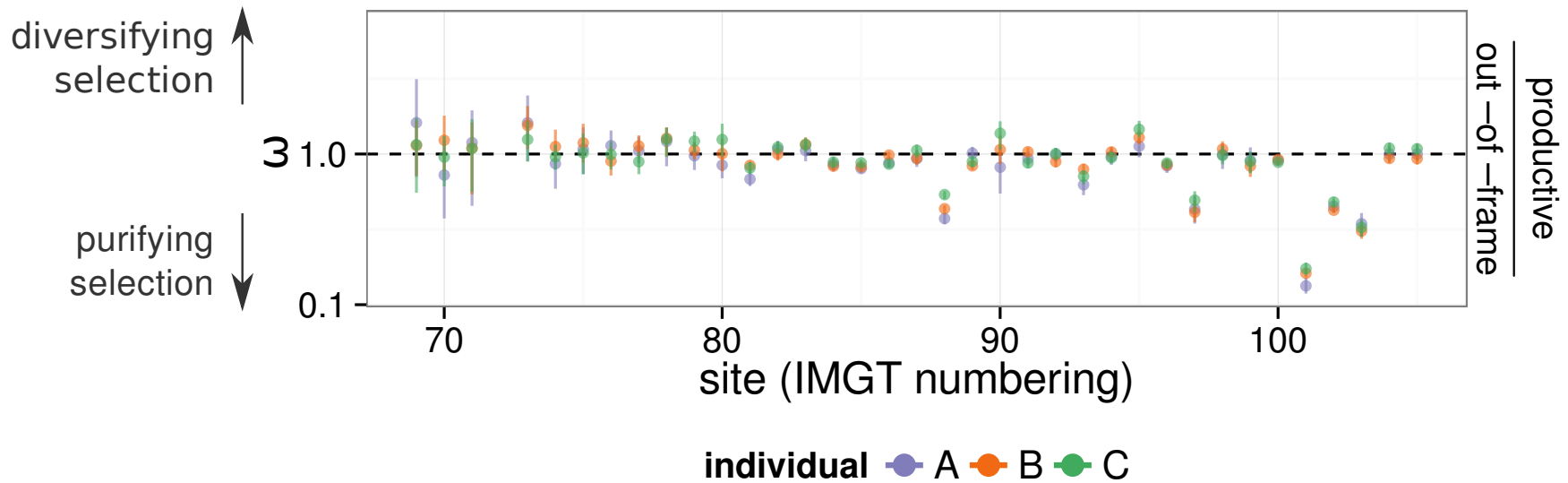
Thr Ile

ACC → ATC  
*nonsynonymous*

This is (natural) selection inference

$$\omega \equiv \frac{dN}{dS} \equiv \frac{\text{rate of non-synonymous substitution}}{\text{rate of synonymous substitution}}$$

We want to estimate this value for each site:



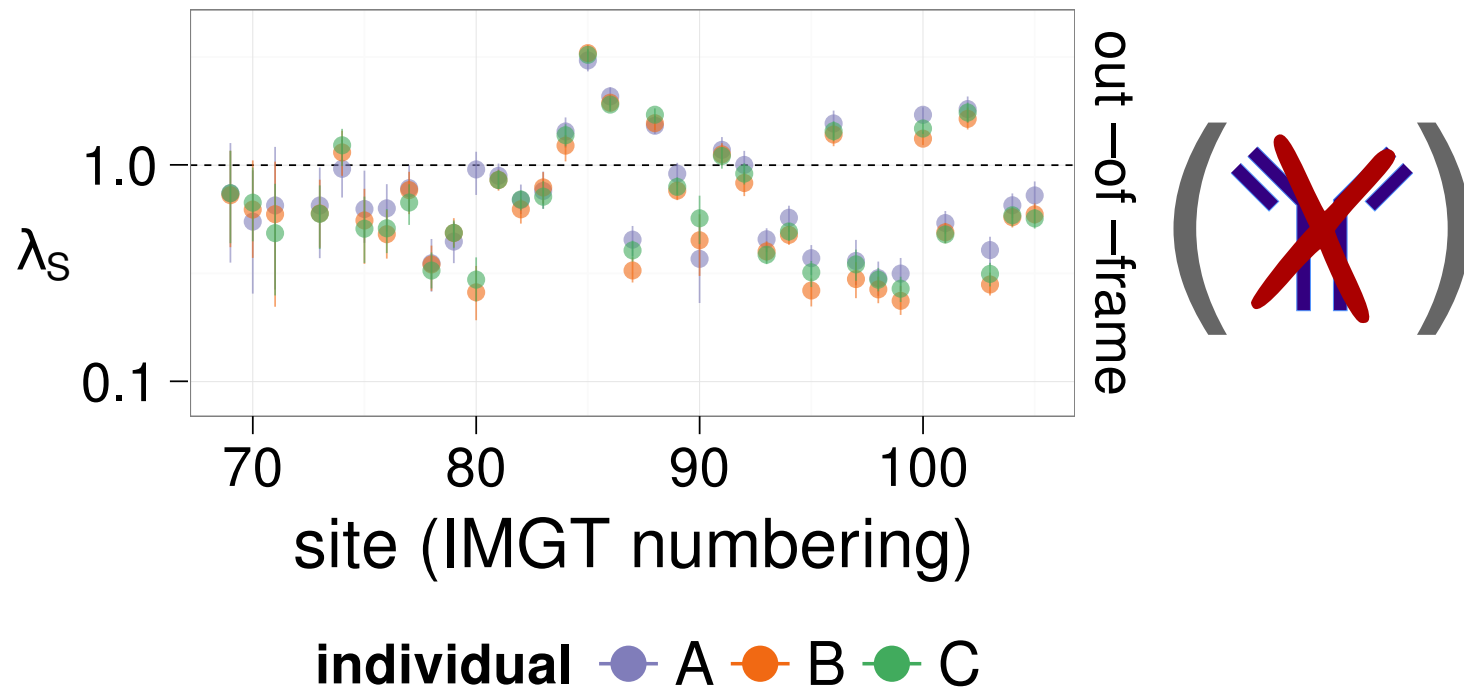
# Challenges

- strange mutational process
- millions of unique sequences  
(rules out otherwise lovely tools like PAML, HYPHY):

*“FUBAR [HYPHY] allows us to analyze larger data sets than other methods: We illustrate this on a large influenza hemagglutinin data set (3,142 sequences)” – Murrell et. al 2013*

# Strange mutational process

Per-site inference is made difficult by a complicated mutation process



*We can use this to tell us about the neutral mutation process.*

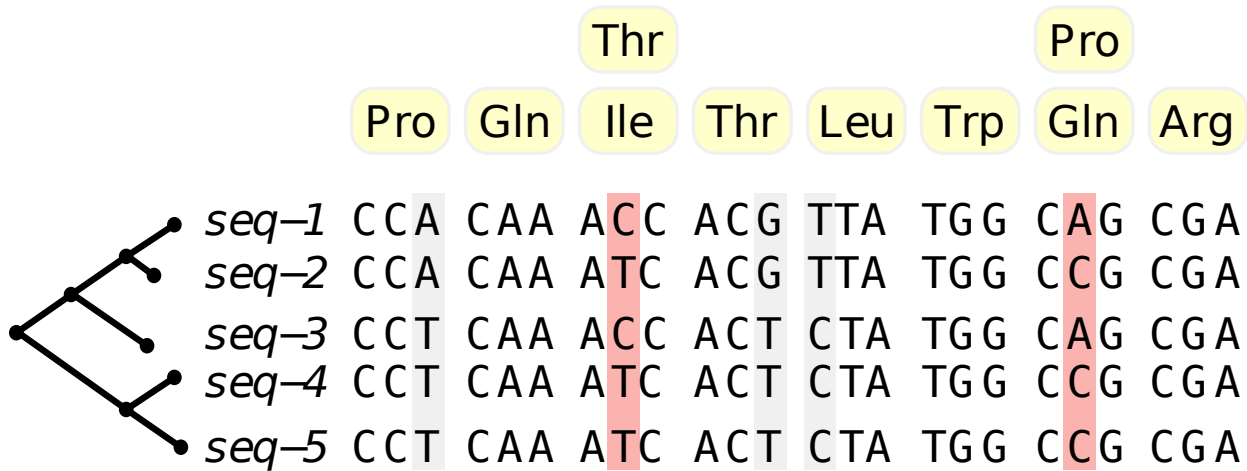
$\omega_l$  is a ratio of rates in terms of observed neutral process

- $\lambda_l^{(N-I)}$  : nonsynonymous in-frame rate for site  $l$
- $\lambda_l^{(N-O)}$  : nonsynonymous out-of-frame rate for site  $l$
- $\lambda_l^{(S-I)}$  : synonymous in-frame rate for site  $l$
- $\lambda_l^{(S-O)}$  : synonymous out-of-frame rate for site  $l$

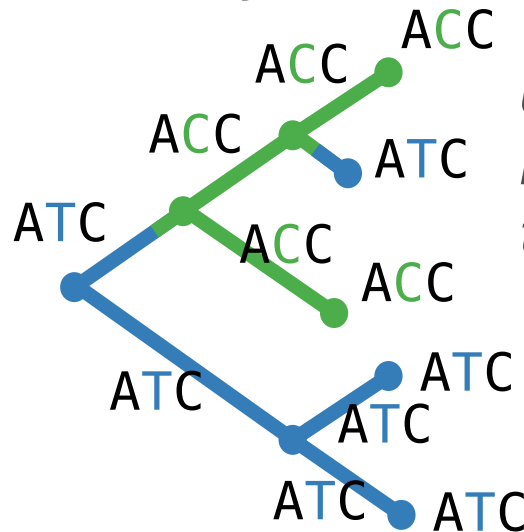
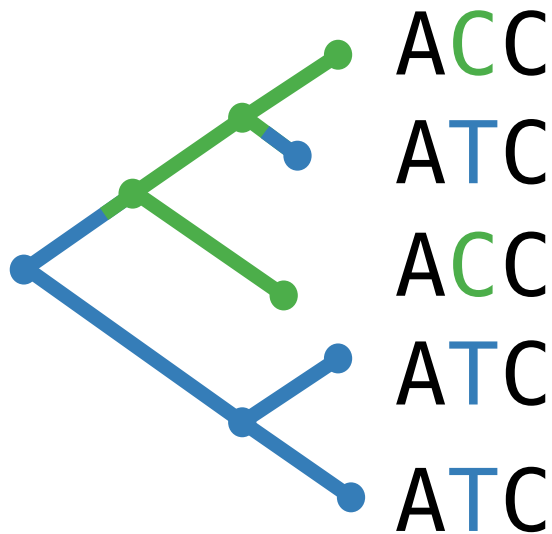
$$\omega_l = \frac{\lambda_l^{(N-I)} / \lambda_l^{(N-O)}}{\lambda_l^{(S-I)} / \lambda_l^{(S-O)}}$$



# Renaissance counting! (Lemey, Minin, ... 2012)



sample ↙ mutation history

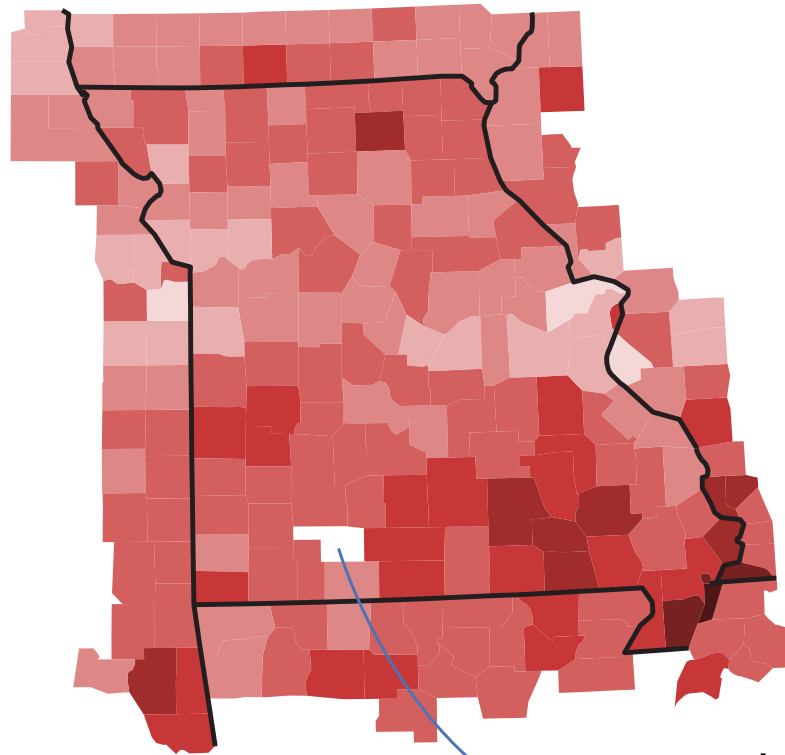


*Use sampled mutation histories to estimate rates...*

*but such estimates can be unstable.*

# Stabilize with empirical Bayes regularization

Say we are doing a per-county smoking survey.



zero smokers? Really?

Use all of the data to fit prior distribution of smoking prevalence, then given observations obtain per-county posterior.

# Stabilize with empirical Bayes regularization

Assume that  $\lambda_l$ , the substitution rate at site  $l$ , comes from a Gamma distribution with shape  $\alpha$  and rate  $\beta$ :

$$\lambda_l \sim \text{Gamma}(\alpha, \beta).$$

Model total substitution counts (sampled via stochastic mapping) for a site as Poisson with rate  $\lambda_l$ :

$$C_l \sim \text{Poisson}(\lambda_l),$$

Fit  $\hat{\alpha}$  and  $\hat{\beta}$  to *all* data, then draw rates  $\lambda_l$  from the posterior:

$$\lambda_l \mid C_l \sim \text{Gamma}(C_l + \hat{\alpha}, 1 + \hat{\beta}).$$

We extended this regularization to case of non-constant coverage.

# Estimating selection coefficient $\omega_l$

- $\lambda_l^{(N-I)}$  : nonsynonymous in-frame rate for site  $l$
- $\lambda_l^{(N-O)}$  : nonsynonymous out-of-frame rate for site  $l$
- $\lambda_l^{(S-I)}$  : synonymous in-frame rate for site  $l$
- $\lambda_l^{(S-O)}$  : synonymous out-of-frame rate for site  $l$

$$\omega_l = \frac{\lambda_l^{(N-I)} / \lambda_l^{(N-O)}}{\lambda_l^{(S-I)} / \lambda_l^{(S-O)}}$$

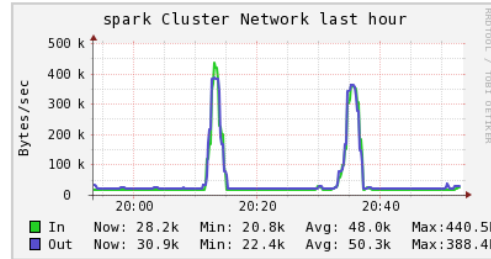
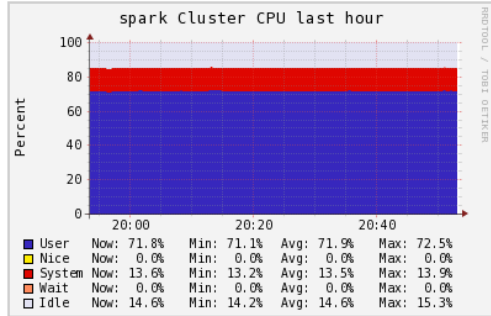
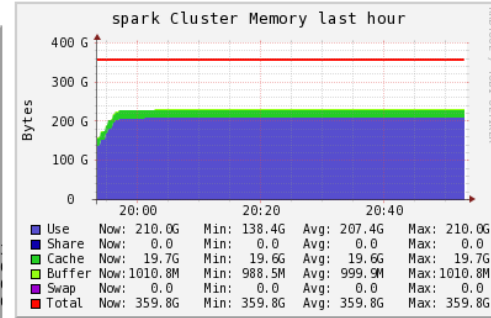
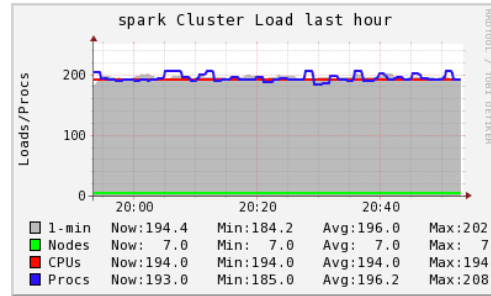
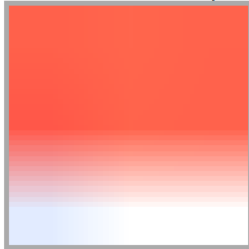
# Used Spark Map-Reduce engine on EC2

## Overview of spark @ 2014-02-27 20:53

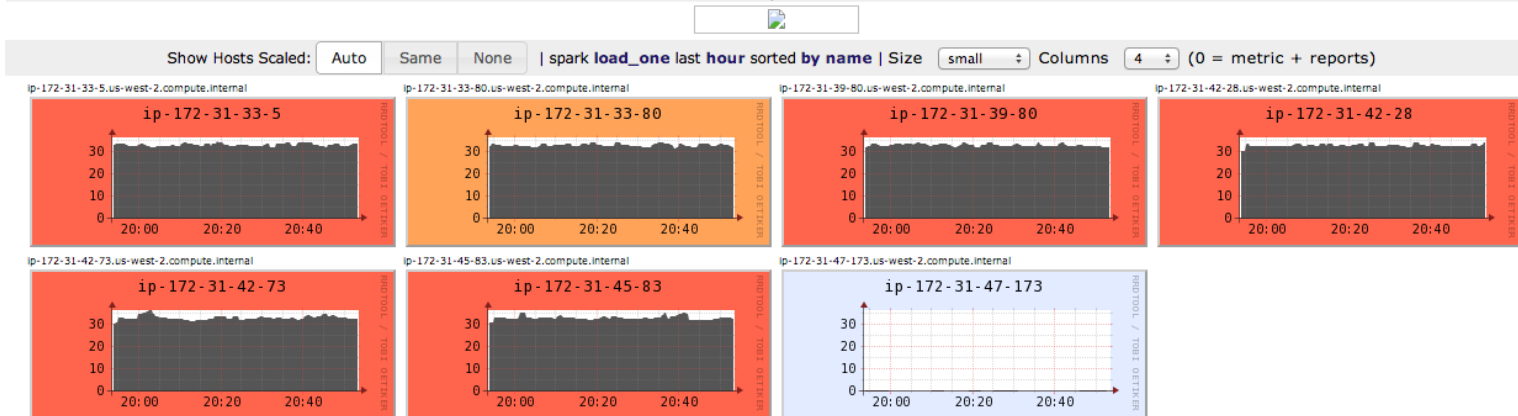
CPU's Total: **194**  
 Hosts up: **7**  
 Hosts down: **0**

Current Load Avg (15, 5, 1m):  
**99%, 101%, 100%**  
 Avg Utilization (last hour):  
**101%**

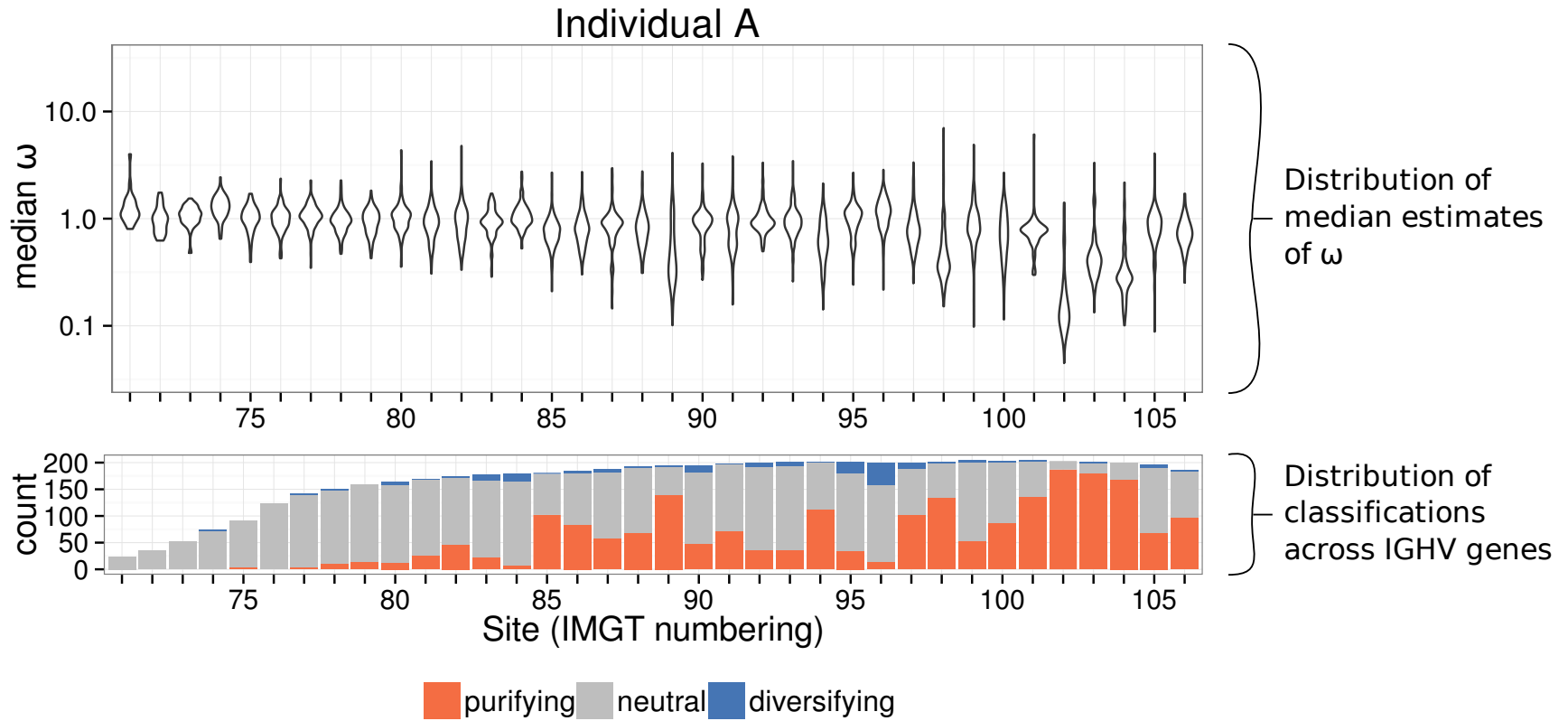
Utilization heatmap



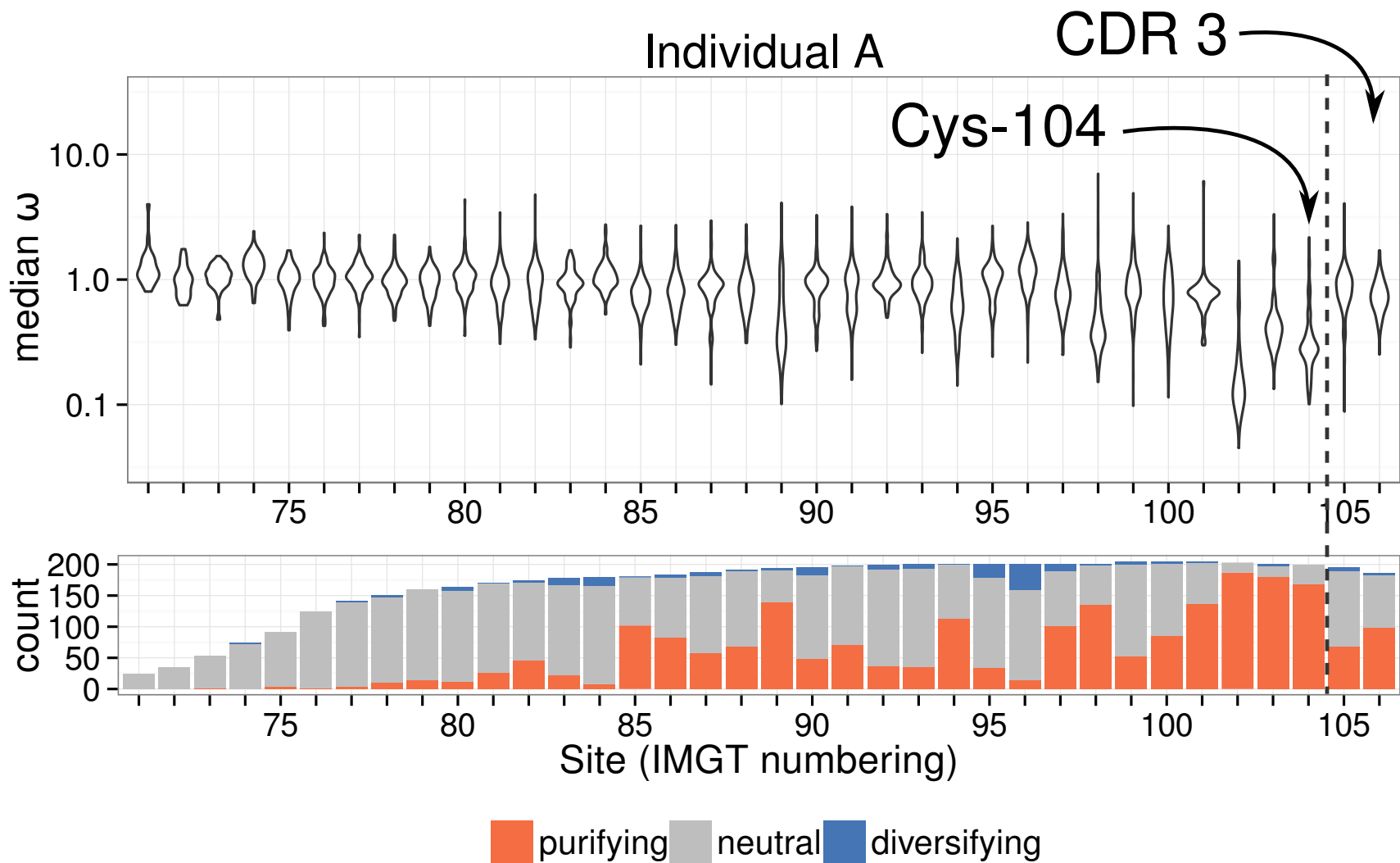
## Stacked Graph - load\_one



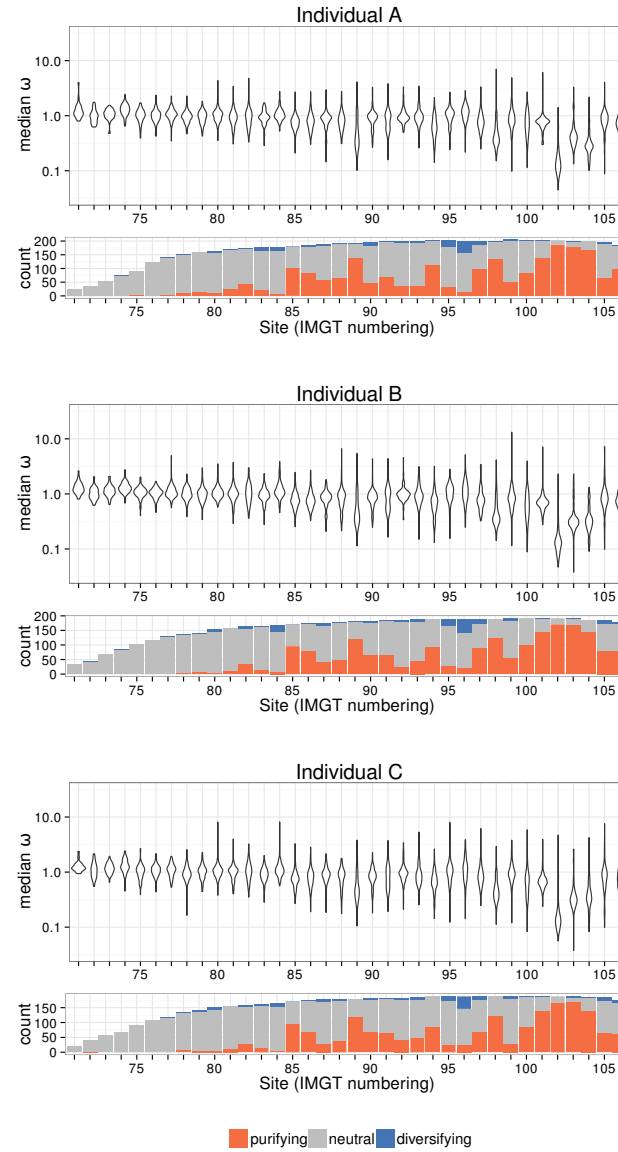
# Overall IGHV selection map



# Purifying selection just before CDR3 loop

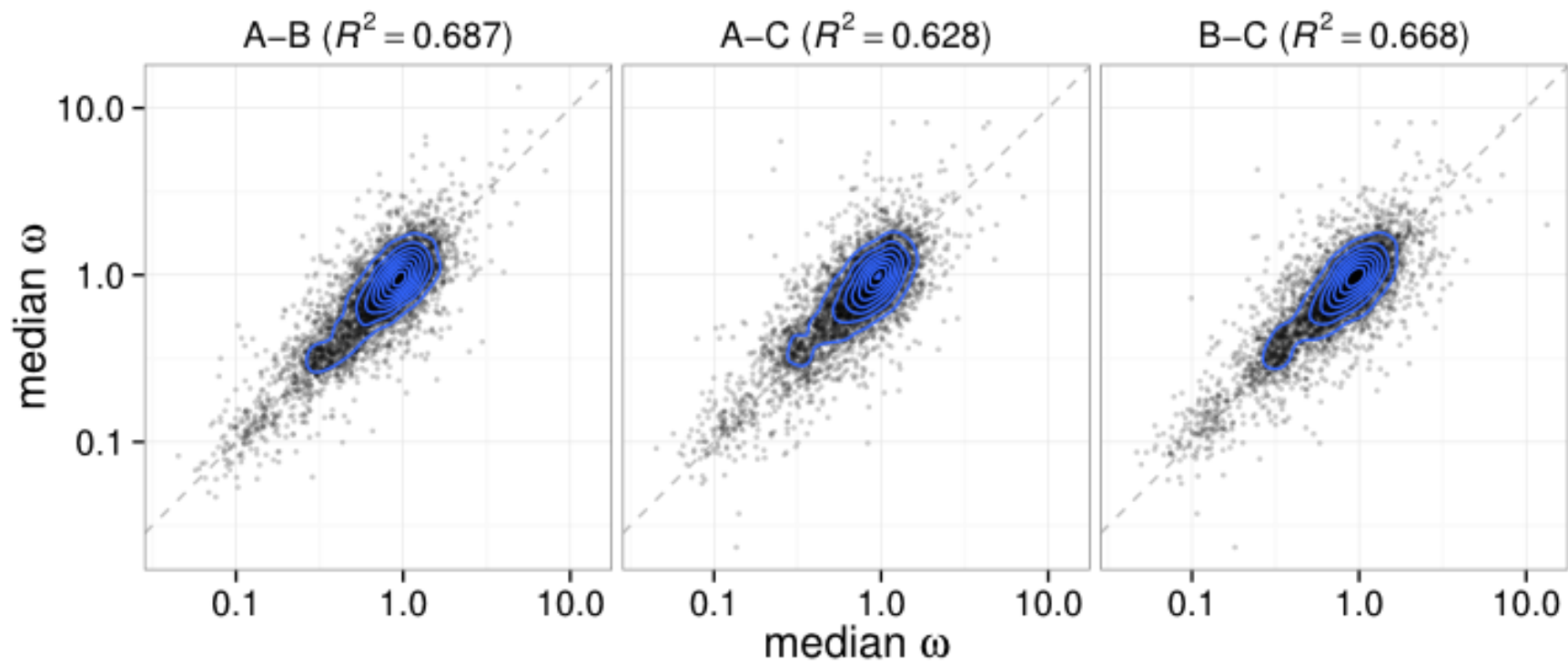


# Similar across individuals

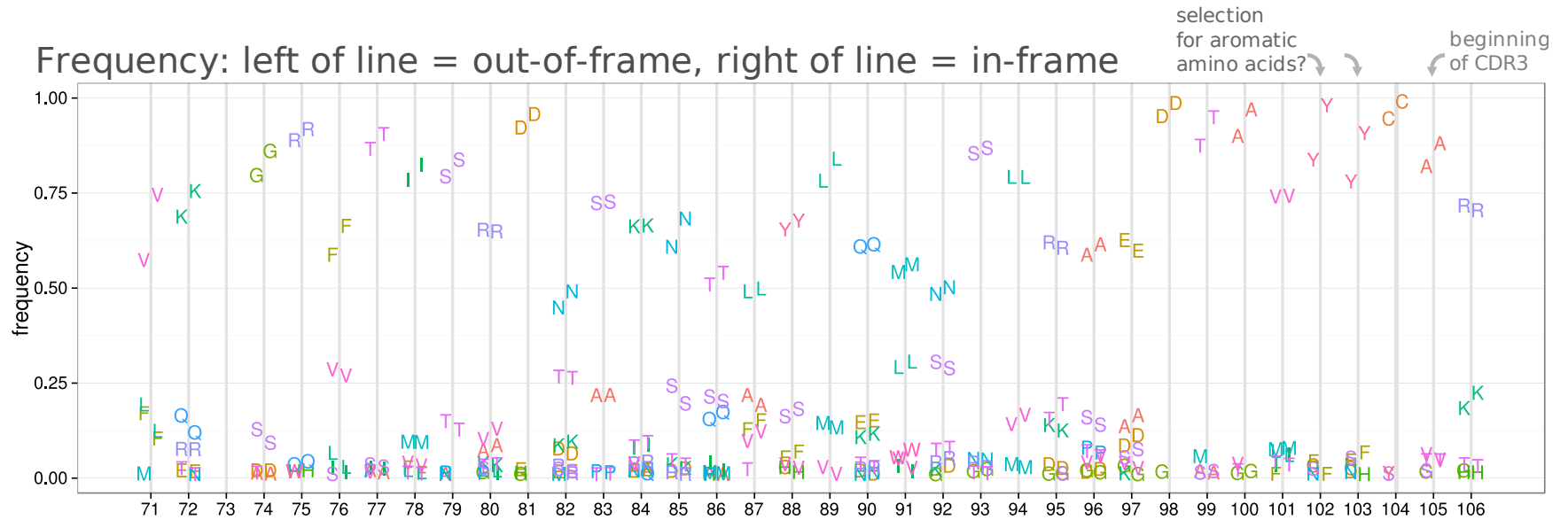




# Similar across individuals (ii)



# Distribution of amino acids



## Wrap-up of part 2

- We developed a **selection inference procedure** that can be used for millions of sequences with non-constant coverage
- We used this to derive a **per-residue selection map**
- We find that **sites are generally under purifying selection**
- We find especially strong selection near the beginning of the CDR3 corresponding to a **preference for aromatic amino acids**

For more details, **paper** is up on arXiv.

**Discuss** on <http://phylobabble.org/>

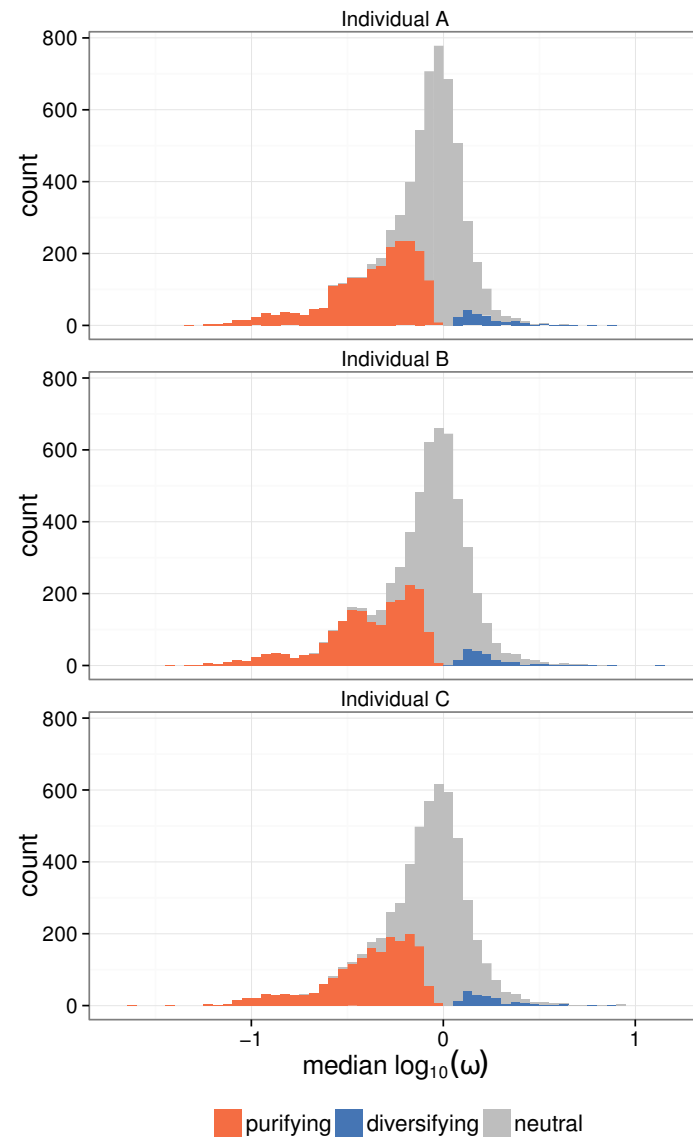
# Thank you

- Connor McCoy, Trevor Bedford, Vladimir Minin, Harlan Robins.
- Molecular work done by Paul Lindau in Phil Greenberg's lab.
  
- W. M. Keck Foundation
- University of Washington Center for AIDS Research (CFAR)
- University of Washington eScience Institute
- National Science Foundation and National Institute of Health

**We have a postdoc opening to work on molecular evolution methods for HIV vaccine experimental design, and probably another for B cell work.**

# Addenda

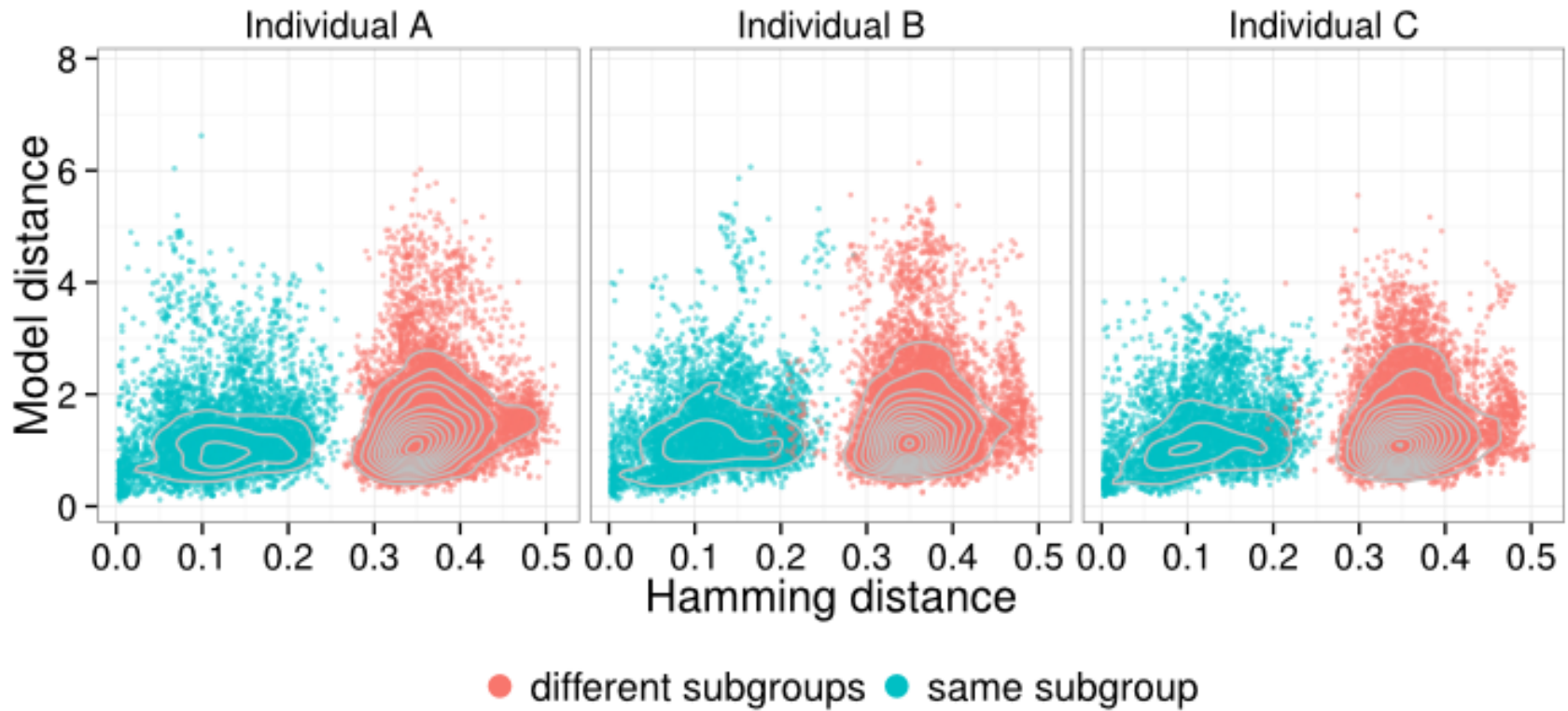
# Sites are generally under purifying selection



# Sequence counts

<b>status</b>	<b>A</b>	<b>B</b>	<b>C</b>
functional	4,139,983	4,861,800	3,748,306
out-of-frame	533,919	794,845	558,246
stop	104,525	169,423	112,901

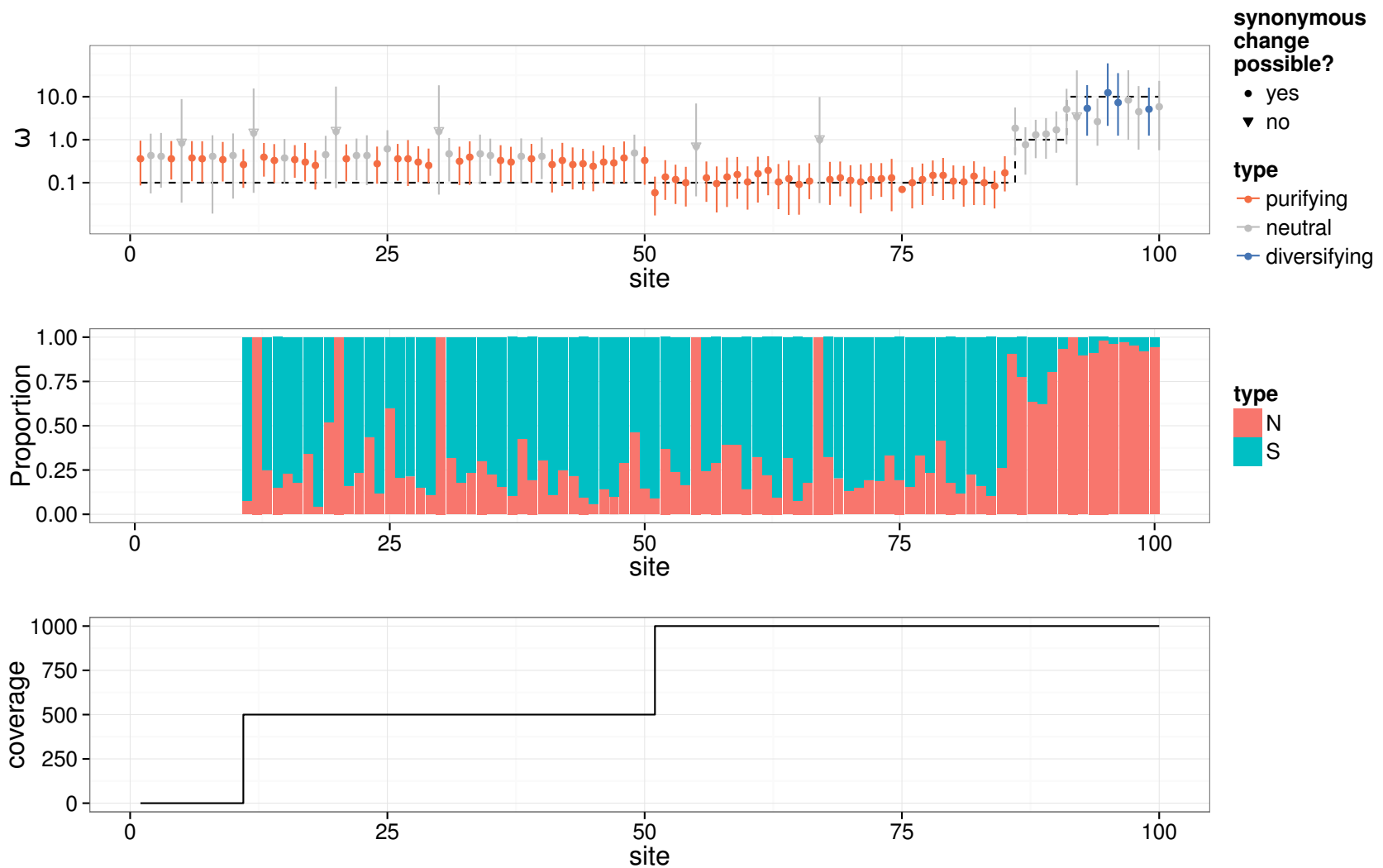
# Correlation between sequence and GTR matrix



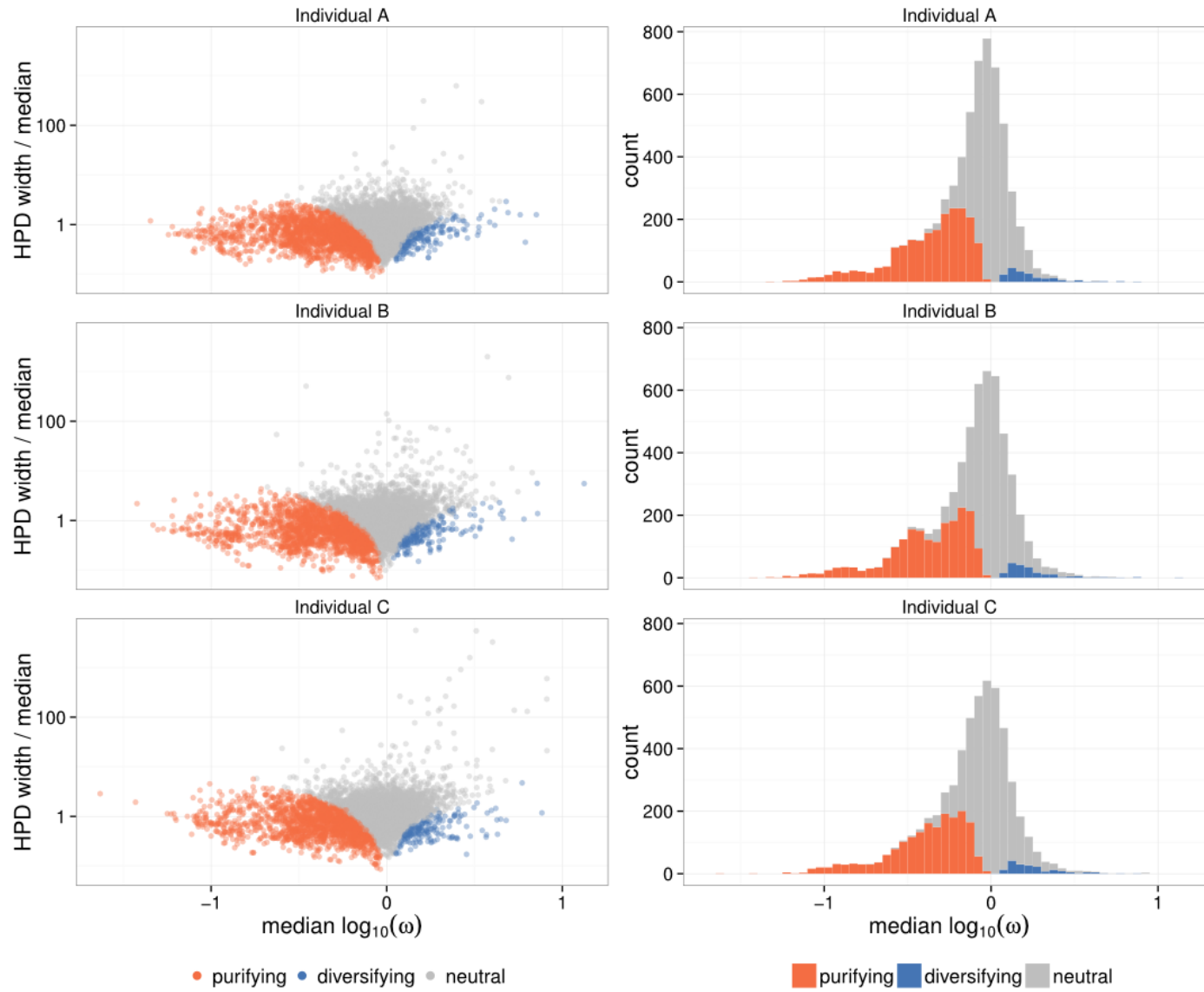
Each dot is a pair of genes.



# Simulation results for selection inference



# Omega distribution



# Random facts

- Mean length of D segment in individual A's naive repertoire is 16.61.
- Subject A's naive sequences were 37% CDR3
- Divergence between the various germ-line V genes:

```
> summary(dist.dna(allele_01, pairwise.deletion=TRUE, model='raw'))  
Min. 1st Qu.  Median    Mean 3rd Qu.    Max.  
0.003846 0.201300 0.344600 0.304700 0.384900 0.539500
```